





# Cross-provider Platoons for Same-day Delivery

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**Keywords:** Platoon, Heterogeneous Groups, Route Matching, Group Building.

**Abstract:** Platooning – vehicles travelling close together behaving as a unit – aims to improve network throughput both on highways and in urban traffic. We study the problem of platoon formation in an urban environment using the scenario of logistic service providers equipped with fleets of autonomously driving pods to carry out same-day delivery tasks by creating cross-provider platoons. The novelty of our work is that we investigate the problem of cross-provider platoons, i.e., platoons with members from different self-interested logistic service providers. Our aim is to study platoon formation mechanisms and possible benefits of cross-provider platooning using simulation. We formulate optimal platoon formation as an integer linear optimisation problem (ILP), aiming to find the longest sub-routes to be shared between vehicles by platooning. The proposed method was implemented and tested on a mesoscopic model to simulate platoon formation and operation, on real network data with realistic background traffic models. Comparing our method to a simpler route matching algorithm reveals comparable system level performance; however, our method performs better with respect to local participant utility, i.e. appears more suited to take vehicle/provider preferences into account.

## 1 INTRODUCTION


With the growth of e- and m-commerce, same-day delivery is emerging as a desirable option for customers. This new logistics concept has been mostly implemented in hub and spoke architectures so far, where delivery satellites are connected with hubs (Crainic, 2008), (Crainic and Sgalambro, 2014), and where last mile delivery is performed from satellite to customer – usually the most costly part of transport (Gevaers et al., 2011).


Logistic service providers (LSP) usually plan and time their deliveries in advance, in order to minimise the driving distance while maximising the number of orders honoured. This process is costly in computational resources and time, thus making it unviable for same day delivery. Orders that are received should be handled immediately, making small-sized, possibly automated vehicles with little capacity a better option not only because of time constraints, but also to achieve higher flexibility in an urban traffic environ-


ment. This creates a huge challenge for LSPs, which are in need of new and innovative ways to successfully complete deliveries in busy urban traffic situations while limiting their own negative effects on it.


Recently, vehicle platooning in conjunction with the use of automated (electric) vehicles has been appearing as a possible technology, enabling more sustainable usage of road space. Starting with early work on highway platooning (Swaroop and Hedrick, 1999) and work focusing on truck platooning and autonomous vehicles (e.g. SARTRE (Robinson et al., 2010)), a considerable body of research on platooning has been recently conducted, including some work studying urban environments. Yet, so far, research on urban platooning has focused on control, stability and operation (see e.g., (Schindler et al., 2018) (Khalifa et al., 2018) (Ali et al., 2015)). There is also some work that considers the use of platooning from a traffic management perspective, e.g., by decreasing congestions and emissions at traffic lights (e.g., (Lioris et al., 2017)).

There is only little research focusing on applying platooning to city logistics applications (e.g. (Scherr et al., 2018)), and to our knowledge; no work that studies methods for platoon formation and operation involving vehicles operated / owned by different ser-

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vice providers, including possible benefits and disadvantages of these methods. For a more detailed account of the state of the art, we refer to Section 2.

Our research aims at closing this gap, and the work described in this paper establishes a first step to investigate benefits and trade-offs of urban cross-provider platooning for same-day delivery. For the scope of this paper, we assume that LSPs operate local fleets of smaller-sized automated delivery vehicles (Pods) which are dispatched into urban traffic. We further assume that platooning is encouraged by traffic management by offering them easier / faster passage through the network. We study methods for platoon formation and operation in this context.

In order to increase the usage (and hence achievable benefit) of platooning in the urban network, we propose cross-provider platoons; that is platoons with vehicles belonging to different LSPs. This leads to heterogeneous groups not only as far as the destinations are concerned, but also – due to the fact that LSPs are self-interested – with respect to constraints, preferences and valuation functions. Platoons are assumed to form spontaneously in the network, and a pod will only join a platoon if its local utility when joining is lower than when traveling alone. Said utility is hereby named costs but measured in terms of time-savings based on traffic density.

In Section 2, we analyse the state of the art and formulate the research gap. In Section 3, we formulate optimal platoon formation as an integer linear optimisation (ILP) problem, aiming to find the longest possible routes to be shared between vehicles. In Section 4, we describe a simulation system implementing the proposed method, and its evaluation against real network data with synthetic but realistic background traffic models. Preliminary results reported in Section 5 are encouraging and show that overall (system-level) performance of our method is comparable to that of state-of-the-art methods, but may lead to higher acceptance by LSPs because it achieves higher average local utility values. We end with a conclusion and outlook in Section 6.

## 2 STATE OF THE ART

### 2.1 Platoons

Platooning – multiple vehicles travelling together as one logical unit – has been getting plenty of attention as of late, since it shows great promise for large freight transport on a highway system (Bengtsson et al., 2015), (Amoozadeh et al., 2015), (Biswas et al., 2006) as far as resource usage is concerned. Platoons

take up less road space since they travel closer together than individual vehicles do, thus positively affecting flow within the network and fuel consumption. The latter is due again, to the smaller gap between vehicles, which in turn reduces wind drag, leading to a lower consumption. This is particularly effective on highways due to the straight roads and high speeds.

Traffic management benefits of platooning have been investigated e.g., by (Lioris et al., 2017), who showed that platoons can increase network throughput at urban intersections and that adapting traffic signalling to allow for the faster passing of platoons can potentially improve overall city traffic.

With regards to urban platooning, related work focuses on models describing ways of control, ensuring stability within the platoon and ways of operation (how vehicles form, travel within and split from the platoon). Ali et al. (Ali et al., 2015) have shown that in order to account for curved roads, as well as varying speeds which tend to occur in an urban network more so than in highway traffic, longitudinal control must be decoupled from the lateral one. They propose three different models, one for each movement type (longitudinal, lateral and platoon). Khalifa et al. (Khalifa et al., 2018) propose a new consensus-based longitudinal control model which is capable of ensuring string stability even in the case of communication breakdown. Schindler et al (Schindler et al., 2018) investigate stable and flexible platooning on urban roads. The authors propose the use of state machines, one for each aspect of the platooning logic (platooning, forming, message, distance).

All previous papers do not address the issue of platoon grouping, which is how the vehicles decide whether to platoon or not and who platoons with whom. Even when discussing joining (Schindler et al., 2018), only the actions leading to forming or joining the platoon are discussed, but not the characteristics which would indicate whether joining/forming makes sense.

Using platooning in the context of logistic same-day delivery is a rather new area of study, where the subject of network design was broached (Scherr et al., 2018). This paper presents how a service network for such a process could be modelled, considering mixed autonomous platoons. The authors consider that fully automated platoons could only be viable on certain parts of the network, and would rely on a human driver to navigate through the others. All vehicles, both human-driven and autonomous belong to a single LSP and focus on minimising the cost of delivery. Even with this study, the subject of grouping vehicles into platoons is not touched upon, mainly due to the homogeneity of the vehicles, and the fact that such

platoons would be grouped and planned to maximise utility in the first place.

## 2.2 Group Formation

When looking at group building algorithms we have different approaches based on the field in which they are applied. More general and largely applied methods are described in (Amir and Lindenbaum, 1998) with algorithms solely based on recognising important information and sorting by a particular criterion (Havaladar et al., 1994); Wertheimers laws of grouping (Gordon, 2004); grouping by maximising a consistency function between group assignment and data; hierarchical grouping (Mojena, 1977); Walds SPRT Algorithm (Wald and Wolfowitz, 1948) or simply by maximum likelihood.

When focusing on vehicle or trips grouping there are again multiple facets, each belonging to a specific domain. To form, maintain and dissolve a group, communication is required; so a clear first grouping strategy would be based on vehicles maintaining communication. (Taleb et al., 2007) state in their paper that a group can be made only by vehicles being able to maintain a communication link and for that they must be grouped by velocity headings. The vehicles must all head in the same direction as well as maintain a constant speed within the group to avoid link breakages due to distance. They assume a very basic set of criteria which is not sufficient for our problem.

Kagaya et al. (Kagaya et al., 1994) present ways to group vehicles with drivers and passengers (some of which with special needs) while also taking into account routing and scheduling. They define their problem as a many-to-many advanced reservation travel problem. They identified different characteristics upon which a group could be built, namely: closeness of desired departure times, the location of origins and destinations, the direction of the trips, the passenger type and trip purpose, number and capacity of available vehicles. Routing and scheduling algorithms often focus on the operating companies by minimising their cost, the length of distance travelled and the empty vehicle travel time/distance. They tend to neglect preferences of the passengers/customers, which should be given more importance. The algorithm proposed by Kagaya works with a fuzzy relation to define similarity of trips. While not exactly the same, a parallel can be drawn between our delivery problem and that of Kagaya. We are less concerned with the human factor, since our vehicles are fully automated, and we have no need to combine trips, since pods cannot exchange packages between them.

Dennisen and Müller (Dennisen and Müller, 2016)

propose preference-based group formation through iterative committee elections. Passengers visiting several points of interest need to be grouped in a ride-sharing autonomous vehicle. They express their preferences on their desired destinations and by iteratively removing the most dissatisfied passenger using the Minisum or Minimax approval committee rules and recounting votes, a suitable grouping is found. In our work, while the goal of finding the best common route is the same, we consider packages instead of passengers. Hence, the voting approach appears less obviously suited to our problem.

## 3 A METHOD FOR CROSS-LSP PLATOON FORMATION

Coming back to our problem of heterogenous group building, we need to identify the important characteristics and limitations that will influence our algorithm. Considering all actors in the traffic scenario, especially logistic traffic, we get different preferences making the problem of heterogeneity more and more complex. We have the clients with the preference of delivery time (delivery window), the pods themselves which have a preferred speed, and an energy budget they must not overdraft (length of route). Then the different providers would want to keep the costs under a certain margin, cooperate with some but not all other competing companies, and also fulfil a certain number of orders per time unit.

A simple implementation of a grouping algorithm to solve our problem of heterogenous group building is to treat it as an optimisation problem based on preferences. All the preferences mentioned above are modelled as constraints in the optimisation problem with the objective of minimising the route costs (thus positively affecting the time and the length of road travelled). The algorithm proposed, presented at length in subsection 3.4, is deterministic and provides one or more "best" solutions.

Employing the previously presented fuzzy theory approach would not be a good fit to the problem simply because the weights given to the criteria are not constant over the different logistics service providers. For some it might be more important to have as many orders fulfilled as possible, thus disregarding platooning as long as it is not immediately available; whereas other might prefer to wait for a platoon instead of travelling alone. So while the set of preferences might contain the same values for all pods (mentioned above), their weight in the decision making process might differ.

In the case where the optimisation problem offers

more than one similar solution (for example in a Manhattan grid scenario), a voting procedure, like the one presented before, could be employed to determine the route and the grouping of pods. This would ensure that route selection is not left up to one entity, but all potential platooning pods contribute to the selection. Such an approach would be a secondary decision mechanism, a fail-safe method to determine a singular solution.

### 3.1 Input

The cities network is transformed into a structure which allows routing; a graph where streets are represented by edges and connecting points by vertices. Traffic demand ( $Q(x,t)$ ) is modelled as a collection of routes given by origin and destination pairs in the network. This represents background traffic, more specifically how many vehicles travel on a specific edge ( $\Delta N$ ) on average in an hour ( $\Delta t$ ). (1) (Treiber and Kesting, 2013).

$$Q(x,t) = \frac{\Delta N}{\Delta t} \quad (1)$$

This is then transformed into traffic density ( $\rho(x,t)$ ), by dividing the number of vehicles per hour ( $\Delta N$ ) through the length of the edge ( $\sum_{\alpha} d_{\alpha}$ ), and added on as that specific edge's weight (2) (Treiber and Kesting, 2013).

$$\rho(x,t) = \frac{\Delta N}{\sum_{\alpha} d_{\alpha}} \quad (2)$$

This will act as our cost to minimise, thus being translated into time-savings; for the more free an edge is, the faster would a vehicle transverse it. Since the pods are electric, the longer they travel and are away from an energy source, the higher the costs of recharging will be in order to dispatch them again.

In the above described environment we add pods and run the optimisation algorithm to determine their routes. The pods have a given destination as well as a set of preferences.

### 3.2 Assumptions

We assume the pods to be functioning independently while also attempting to form a platoon. A platoon can be formed by two or more pods. It can only form at intersections in the network. Platoons form spontaneously. Pods must not only be at the same place in order to platoon but also in the same time space. A pod only joins a platoon if the expected platooning cost is lower than that of travelling alone and all its restrictions respected. After formation, pods travel in a platoon with a uniform speed.

Short range communication must be present. The pods communicate with a local agent which performs the optimisation algorithm. Lastly, it communicates the groups, common route, length and expected costs back to the pods.

Platooning is encouraged by traffic management, through treating platoons as **one** entity, exactly like a vehicle would be. Thus, the members of a platoon all contribute to the cost of a route. We assume the cost of the route to be the sum of the traffic density on all edges taken. When travelling in a platoon, all participants contribute equally with the same amount. This naturally reduces the cost of the whole route for all participating pods and encourages the formation of larger platoons.

### 3.3 Definitions

In Table 1 we introduce the basic symbols used in the formalisation of the optimisation problem, and their meaning:

Table 1: Symbols and meaning.

Symbol	Definitions
$G=(V, E)$	graph
$n \in V$	vertices
$e \in E$	edges, $e \equiv (i, j)$
$d(e)$	traffic density of edge $e$
$l(e)$	length of edge $e$
$dest$	destination vertex of a pod, fixed
$c(e)$	cost of a pod to transverse edge $e$
$K_v^*$	costs of alone travel for pod $v$
$\Omega_v$	maximum delivery time for pod $v$
$\Lambda_v$	maximum length of route for pod $v$
$p(e)_v$	price pod $v$ pays for edge $e$
$NP$	the number of pods in the platoon

### 3.4 Optimisation Problem

The goal of the optimisation problem is to have the longest overlapping route for all pods, all the while taking into account their particular preferences. This can be written as an adapted shortest path problem.

$$\min \sum_{(i,j) \in E} x(i,j) * c(i,j)$$

$$x(i,j) \in \{0, 1\} \forall edge (i,j)$$

$$\sum_j x(i,j) - \sum_j x(j,i) = \begin{cases} 1 & \iff i = Origin \\ -1 & \iff i = Destination \\ 0 & otherwise. \end{cases}$$

The variable  $x$  indicates whether the edge denoted by the vertices  $i$  and  $j$  is used in the shortest path

(value of one) or not (value of zero). The three cases represent the flow constrain which ensures that the route flows through intermediary vertices. Then the objective function reduces the costs to a minimum.

In the case of platooning, we have to add in a new variable to cover all routes for all pods, namely  $y$ . Much like  $x$  it will have the value of one if it is included in the route of any pod, or zero if it is not. This is the variable that replaces  $x$  in the objective function. The flow constraint remains the same, and we add one more to ensure that  $y$  takes the value of one **only** when one or more  $x$  for that specific edge has the value of one.

This leads us to the formulation of the platooning optimisation problem:

Given a group of pods  $Pods$ , being at the same vertex  $O$  in the graph at the same time; let the routes for all the pods be given by  $y(i, j)$ , and the individual pod routes by  $x(i, j)_v$  where

$$\begin{aligned} & \min \sum_{(i,j) \in E} y(i, j) * d(i, j) \\ & y(i, j), x(i, j) \in \{0, 1\}, \forall edge (i, j) \\ & x(i, j)_v \leq y(i, j) \forall edge (i, j), \forall pod v \\ & \sum_j x(i, j)_v - \sum_j x(j, i)_v = \begin{cases} 1 & \iff i = O \\ -1 & \iff i = dest_v \\ 0 & otherwise. \end{cases} \\ & \forall v \in Pods, \forall (i, j) \in E \end{aligned}$$

Preferences are modelled as restrictions in the optimisation problem, so in addition to the base problem presented previously, one could add

$\sum_{(i,j):x(i,j)_v=1} c(i, j) \leq K_v^*, \forall pod v$ , cost restrictions

$\sum_{x(i,j)_v=1} l(i, j) \leq \Lambda_v \forall pod v$ , length of route restrictions

$\sum_{x(i,j)_v=1} \frac{l(i,j)}{s} \leq \Omega_v \forall pod v$ , time restrictions (delivery-window)

and so on.

To incentivise the pods to form a platoon we grant vehicles a reduction in costs; the more pod in a platoon, the lower the cost of the edge is. In this paper's case, it is equal across all pods forming the platoon. Therefore we get

$$p(i, j)_v = \frac{c(e)}{NP} \forall pod v$$

$$p(i, j)_v \geq 0 \forall vehicle v \text{ and edge } (i, j)$$

and the previous cost restriction becomes

$$\sum_{(i,j):x(i,j)_v=1} p(i, j)_v \leq K_v^*, \forall pod v.$$

## 4 SIMULATION

### 4.1 Overall Architecture

The simulation kicks off with loading the environment and starting the internal clock. Then the pods would be generated, either at specific locations (delivery satellites) or random ones, given a destination and a set of characteristics and preferences. The pods follow the best route toward their destination while also attempting to build platoons. If pods/ pods and a platoon/ platoons, meet at the same vertex, they communicate their destination and preferences to a centralised agent situated at that vertex, which runs the aforementioned optimisation algorithm. Alternatively, a pod may choose to wait to form or join a platoon, and communicates the necessary information upon arrival at the vertex. The algorithm provides the groups, common route and expected costs for all pods.

After the pods are grouped in a platoon, they follow the common route until its end, then disband and continue toward their destination. To accommodate the fickle nature of urban traffic, the platoon may be re-routed at each intermediary vertex. The simulation ends when all pods have successfully reached their destination.

### 4.2 Implementation

To execute and run the program, a simulation was built using Java. For each of the components of the simulation an appropriate framework was found and used. For the environment we used Jung (O'Madadhain et al., 2018) a powerful and flexible library to model data into a network or a graph. It comes with routing and analysis algorithms, as well as additional libraries for visualisation purposes. To help with visualisation of the routes, we use a heat map. This is built using colour maps, kindly provided by (Kraus, 2018). A JXMapView2 (Steiger, 2012) painter was defined, based on existing examples, to draw the routes.

The optimisation method is executed using the commercial solver Gurobi (Gurobi, 2018), chosen since it can be easily introduced in a Java program as a Jar file. The process of defining the problem goes as follows; at first, the optimisation environment and

model are defined. Based on the number of pods in our theoretical platoon, several  $x$ 's as well as one  $y$  are defined as binary variables for each of the edges in the graph. When creating the  $y$  variables, the objective function is also defined. The next step is to add the constraints; first is the flow constraint, which is defined for each of the pods; then the  $x \leq y$  constraint, and lastly, whichever preference constraints the user deems as necessary. In the infancy stages of the project we just used the length constraint, forcing pods to not take detours longer than a *given coefficient*  $\times$  their ideal shortest path. The model is then optimised, the results saved into another data structure and the model then made redundant. The results can be displayed anytime by calling the display function.

In order to be able to compare our optimisation approach with a state-of-the-art alternative, we conceived a baseline algorithm, which creates an overlap of all the pods' best routes. Assuming the current position of the pods as the origin point, the best (fastest) route is identified with a normal routing algorithm. After a route has been found for all pods, they are aggregated, and the number of times an edge appear in a route, counted. This gives the number of pods per edge, giving a crude approximation of where a platoon could form and who could be a part of it. This approach is fairly straightforward and easy to calculate, but does not take into account all the possible restrictions and preferences that may arise.

### 4.3 Simulation Settings and Input Data

The data acting as the environment for our simulation can be found at <https://github.com/bstabler/TransportationNetworks> (Stabler et al., 2018). We focused on the Berlin neighbourhoods since they were the most finely granular example provided. The network was transformed into a Json file respecting a Json schema defined for this specific purpose.

Traffic demand was not given along with the networks but had to be generated based on trips between given zones. The vertices were divided into zones which were provided in the trips file. To simulate the trips given, random vertices were pulled from each zone and then the best route between them calculated. For example, if there were 14 trips from zone 1 to zone 8, the process would be as follows: pull a random vertex from zone 1, pull a random vertex from zone 8, route, save the edges taken. Repeat this process for another 13 times. All the resulting routes were aggregated and divided by the edges' length giving us the traffic density which is then added in the form of edge weights to the environment. The results

from this process are not constant, but they are similar enough to be consistent throughout the runs.

### 4.4 Simulation Output

A simulation run delivers two types of outputs. The *first* is a visualisation of the network, with edges painted to represent how many pods travel on them, in the form of a heat map. The colour range chosen to display the heat map was the Inferno palette since the spectrum (yellow for hot to dark purple for cold) is uniformly perceived and understood by the human eye. (Thyng et al., 2016) Thus, a light yellow coloured edge would indicate that all pods would use that edge, whereas a dark purple edge would mean that it is a part of only one pods' route. An edge with no colour means that it is not used in any of the routes.



Figure 1: Heat scale.

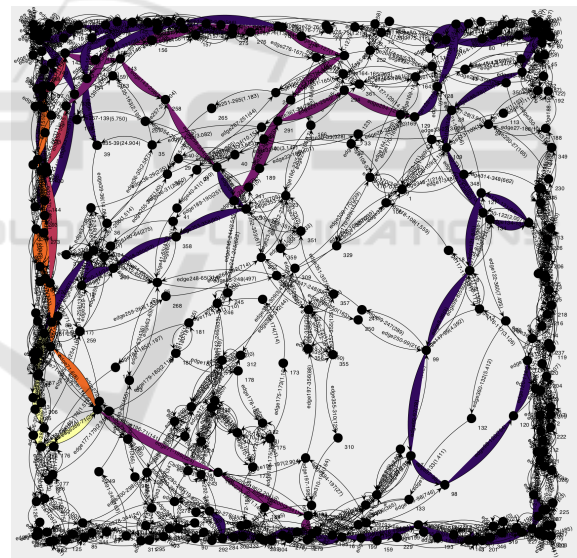


Figure 2: Route for a ten pod platoon, on real Berlin network. For legend see Figure 1.

The *second* output is a log file consisting of six parts:

1. the origin and destination vertices. These are given to help with the understanding and interpretation of results.
2. the routes of individual pods. Since the individual route is also given by the optimisation function; the list of  $x$ s with the value one is displayed for each of the pods/destinations.

3. the route of the fleet. The  $y_s$  with the value of one are also displayed, thus rendering the route of the whole fleet.
4. the number of pods per edge. For each of the edges displayed in step three, we get the number of pods which would travel it.
5. the cost savings. For each of the destinations, the original costs (travelling alone) are displayed along with the new costs if the pods were to platoon how the optimiser suggests.
6. the system optimal solution costs, i.e. the sum of the weights of all edges mentioned in step three.

The baseline algorithm follows the same structure, creating first a heat map visualisation of the network and then presenting written results following the same 6 step pattern as before.

## 5 RESULTS

Experiments were run on a set of real and synthetic environments using both realistic and generalised background traffic density. For the real environments we used the Berlin networks mentioned in Chapter 4 coupled with realistic traffic density data. For the synthetic environments a simple five by five vertex Manhattan grid was created with higher traffic density on the outside edges and lower in the center of the network. The algorithm was run both with and without restrictions (preferences), in our experiments case length of route and cost restrictions, performing well. All common routes could be determined and the number of pods in the platoon specified.

When studying the resulting heat maps, one can easily identify potential split and also join points in the routes. Whenever the colour changes to colder it means pods would leave the platoon and whenever it would get warmer, pods would potentially join the platoon. For ease of visualisation and understanding, the remaining figures exemplifying results will be shown on a smaller synthetic environment with lower edge weights in the center and higher on the outside.

To identify join points, we must assume that two groups of pods are platooning from different origins and spontaneously meet at a different vertex in the network. If their routes have a common set of edges, they may choose to form an even larger platoon. To illustrate we have the following example presented in figures 4, 5 and 6. Each of the problems has a separate instance of the optimisation algorithm set as their route, and upon meeting, would run another one to determine the combined platoon.

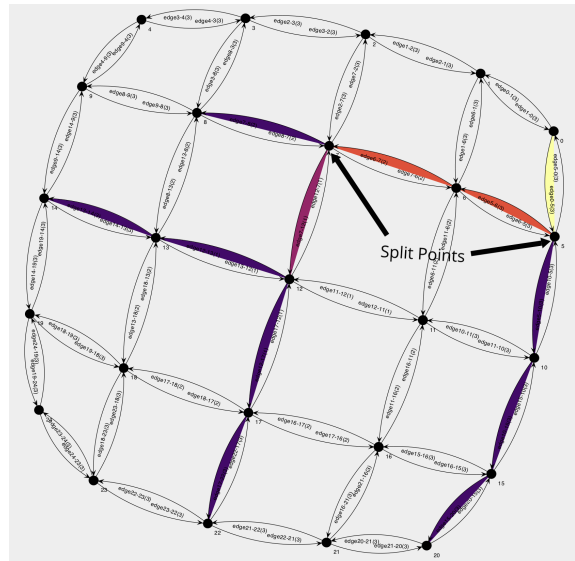


Figure 3: Route for five pods, synthetic network, featuring split points. For legend see Figure 1.

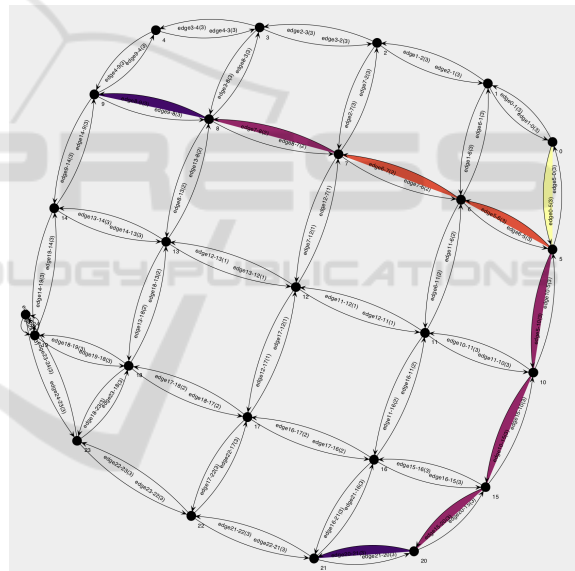


Figure 4: Route for five pods, synthetic network, starting vertex 0. For legend see Figure 1.

We can see that the two problems (Figures 4 and 5), have edges 7-8 and 8-9 in common, so vertex 7 could act as a join point. Here a four pod platoon could be created, with two pods pertaining to the platoon starting from vertex 0 and two other from the platoon starting from vertex 2 (Figure 6).

### 5.1 Comparison to Baseline Algorithm

To illustrate this we go back to our real-life example of the Berlin Tiergarten neighbourhood. To mimic

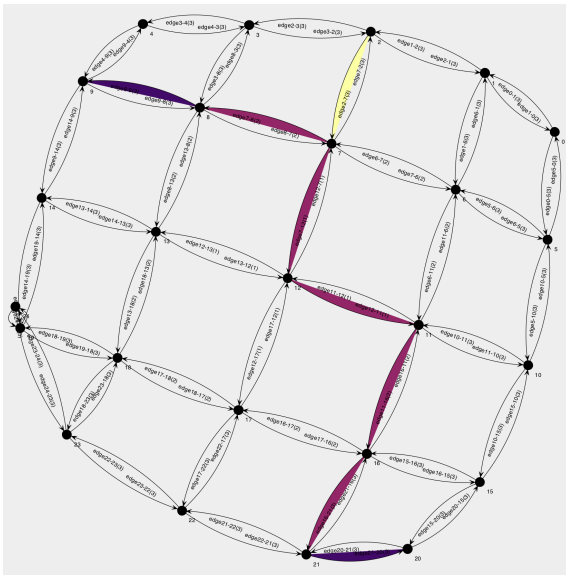


Figure 5: Route for five pods, synthetic network, starting vertex 2. For legend see Figure 1.



Figure 6: Route for ten pods, synthetic network, two starting vertices, featuring join point. For legend see Figure 1.

real traffic, we assumed the pods would meet at the most popular intersection (where most traffic takes place) and considered that our origin point. For the destinations, we selected the vertices where the subtraction of entering and exiting vehicles was the lowest. With these origin-destination pairs we performed both algorithms and studied their results as far as costs are concerned. In Table 2 the results are presented; the first column denotes how many pods meet and could platoon, the second and third column present the overall costs for the overlapping and optimiser algorithms

respectively. The fourth column presents the pods, and the last four columns show their costs; if they were to travel alone, platooning by the overlapping solution, platooning by the optimiser solution, and finally the cost of the tour with the optimiser solution without the platooning incentives.

In some cases, especially for smaller platoons, the algorithms deliver the same solution, like the case presented with six pods. With eight or ten pods we see how the optimisation algorithm produces a better solution than the simplistic algorithm. This is due to the fact that the resulting route from the optimiser presents the system optimal solution; providing the longest, but most cost-efficient common route of the pods. When looking into the simple overlapping example, we get the pod specific optimal solution, which is to be expected.

We can also see, in the case of pod v8 for both of the last cases, that in our optimiser approach it is included in a platoon, whereas for the overlapping one it travels alone.

Although one can see that the overlapping solution provides more cost savings for individual pods, its simplistic method would not be suitable as a complete solution, since the preferences cannot be modelled in. The optimiser approach treats preferences as restrictions on the system and would provide a more complete solution to the platooning problem.

## 5.2 Runtime Performance Analysis

As far as performance of the algorithm is concerned, the runtime increases exponentially with the number of pods as expected, but due to the nature of our scenario this bears little importance. In a traffic scenario where the pods must be close in both space and time, we do not foresee more than twenty individual pods forming a platoon. In the case where more platoons would join forming a larger one, they still act as individual pods, thus keeping the optimisation problem small. Even though the optimisation approach is substantially slower, it still performs within an acceptable margin of 23 seconds for fifty pods. For a more realistic scenario of five or ten pods, it performs in 2.8 and 3.7 seconds respectively.

In Figure 7 both algorithms' performance is portrayed, with each point representing the runtime of one instance of the optimisation problem / overlapping algorithm respectively for the number of vehicles specified.



Table 2: Resulting costs comparison of the two algorithms. Costs represented in traffic density, measured in number of vehicles per length unit of the edge.

Pods	Total Overlap	Total Optimiser	Pods	Alone-travel	Overlap	Optimiser	Tour
6	51954	51954	v1	3510	1010.58	1010.58	3510
			v2	4818	2318.58	2318.58	4818
			v3	5765	3508.58	3508.58	5765
			v4	16578	16329.5	16329.5	16578
			v5	30702	28538.25	25538.25	30702
			v6	497	248.5	248.5	497
8	75103	73161	v1	3510	773.75	880.3	3510
			v2	4818	2033.25	3265.5	6868
			v3	5765	3352.75	3378.3	5765
			v4	16578	16329.5	16329.5	16578
			v5	30702	28394	28408	30702
			v6	497	248.5	248.5	497
			v7	16330	13545.25	13700.3	16330
			v8	10426	10426	6950.5	10553
10	119682	98455	v1	3510	677.58	880.3	3510
			v2	4818	1937.08	3265.5	6868
			v3	5765	3256.58	3378.3	5765
			v4	16578	16274.3	5484	16578
			v5	30702	24762.83	28408	30702
			v6	497	193.3	124.25	497
			v7	16330	13449.08	13700.3	16330
			v8	10426	10426	6950.5	10553
			v9	25113	24892	11066.38	27742
			v10	29752	23812.83	25186.58	41862

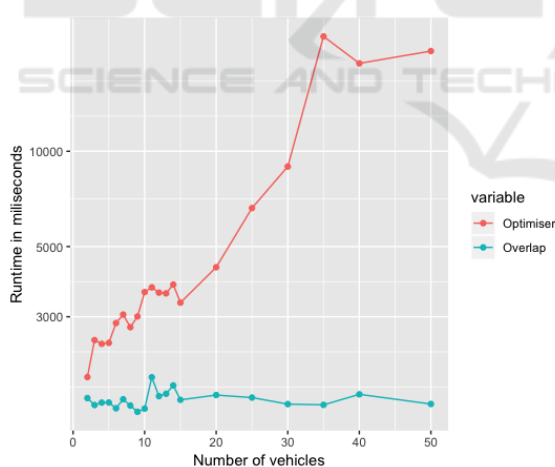


Figure 7: Comparing the two performances.

### 5.3 Discussion

Overall the algorithm performs well and gives a viable route and a possible grouping for the pods to platoon. It provides the system optimal route, which may not guarantee the best individual cost savings for the pods, but a substantial cost saving nevertheless. When dealing with a heterogenous group, an individual optimal solution would most likely mean that the

pod is not part of the group, and since costs are equal across all pods, the system optimum is the individual optimum as well. The optimisation method is simple, easy to understand and to use, however it may prove to be slow when comparing to other more novel approaches. It makes up for it though, by being a very straight forward and precise way of including preferences into the routing and grouping algorithm.

The next steps of this research, are to complete this program creating a fully functioning simulation, including discrete time and moveable pods in the environment. With the inclusion of time, more restrictions can be added (such as delivery windows and speed) thus adding another degree of realism to the results. To further improve on the accuracy of the simulation, we plan on using more real cities with exact visualisation by means of Graphhopper (Karich et al., 2018) and Open Street Map (OpenStreetMap, 2018). This information is readily available and easy to implement but traffic density data is scarce and hard to find.

This application will then be further developed into a fully fledged agent-based simulation of urban logistic traffic, which is immensely useful in the further research on urban platooning.

## 6 CONCLUSION

Using self driving electric vehicles to carry out package deliveries in cities is a logical next step for logistic companies. Not only do they cut costs on employing human drivers, but they also cut down on harmful emissions in an already polluted environment. Given that these vehicles are small for the time being, they can only carry one or very few packages in one trip. Having many such vehicles swarming an already overcrowded network would be chaotic and confusing, so for their sake as well as the general traffic, they could form platoons and travel in a convoy.

To ensure that groups are formed, all pods are viable for platooning, but can impose certain limitations, whether they are characteristics (such as speed), restrictions (must arrive at their destination by a specific time) or preferences (would platoon with some but not all other pods).

This paper presents a simple and flexible algorithm in order to create cross-provider platoons of autonomous electric pods used for same day delivery. Routing and grouping are handled by an optimisation problem, treating features and preferences as restrictions. The objective function is minimising the platoons cost, which is modelled as traffic density for each edge transversed. The aforementioned characteristics and limitations are represented by linear constraints. This offers more freedom to add or limit the system without much difficulty, all the while maintaining a clear and optimal result.

The program performs well and is accurate even with a large number of vehicles, giving not only the route of the platoon, but each individual pods route as well.

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