

Plane Equation Features in Depth Sensor Tracking

Mika Taskinen, Tero Sääntti and Teijo Lehtonen

University of Turku, Department of Future Technologies, 20014 Turun Yliopisto, Finland

Keywords: Depth, Sensor, Plane, Equation, Tracking, 3D, Augmented Reality.

Abstract: The emergence of depth sensors has made it possible to track not only monocular cues but also the actual depth values of the environment. This is especially useful in augmented reality solutions, where the position and orientation (pose) of the observer need to be accurately determined. Depth sensors have usually been used in augmented reality as mesh builders and in some cases as feature extractors for tracking. These methods are usually extensive and designed to operate by itself or in cooperation with other methods. We propose a systematic light-weight algorithm to supplement other mechanisms and we test it against a random algorithm and ground truth.

1 INTRODUCTION

Today the use of augmented reality solutions is increasing and more efficient methods for tracking are being developed for motion sensors and conventional cameras. Using depth sensors in this manner is a fairly new area, in comparison as they have not been accurate or mobile enough to be used in augmented reality. Over the last few years this has changed drastically and now some algorithms and methods have finally been researched for the depth sensors.

All sensors have their faults when tracking the pose. A conventional camera might lose its track when the captured image lacks details. Motion sensor has to be accurate and record data in high frequency. Even then the pose might drift unless corrected with other methods. A depth sensor usually does not work under sunlight conditions or when the distance to the tracked surroundings is too great. These, and possibly other methods, need to be combined to achieve more robust tracking.

The advantage of depth sensors in tracking is the actual depth data which contains real distances to target areas. These distances can be used to isolate basic formations like planes, cubes and spheres. The data can also be used when building up a more robust model of the surroundings.

Currently the depth sensors are mostly used to map the surroundings of the user and tracking is usually done by a combination of motion sensors, conventional cameras and location services. Some tools

for depth tracking exist, but as of yet, their usage has been limited. As a scanning feature, Microsoft has introduced KinectFusion to be used with Kinect to scan objects with limited space requirements and limited depth tracking abilities (Newcombe et al., 2011). A plane filtering method with Ransac (random) feature selection system has been suggested to fully implement depth sensor tracking (Biswas and Veloso, 2012).

Due to the current limitations of the depth sensors in range and accuracy, a lighter and more systematic feature and tracking algorithm is proposed to support other tracking mechanisms. By keeping features as plane equations, no real edges and corners are detected, only intersections between infinite planes. This makes the algorithm much faster than an algorithm that uses computing power to detect physical edges. Systematic detection makes plane equation tracking a more adjustable tool while giving possibility to increase robustness. Changing the grid size can be done on the fly, and it provides an easy tradeoff between execution time and accuracy.

The paper is organized as follows: The paper begins with introduction where we lead the reader into the subject by presenting the problem. Next section, *Related Work*, gathers references to other papers and methods to explain the current state of the development. The *Plane Equation Detection* section introduces the solution (algorithm) with operation flow and equations describing the entire method step-by-step. We have tested our process against another one

and show the technical readings in depth in *Results*. The *Discussion* section covers additional ideas, like tracking, to further develop the solution. The final section, *Conclusions*, summarizes the paper and the results overall.

2 RELATED WORK

The plane equation method is not the first idea involving depth sensors and tracking since the sensors have become consumer products. Other propositions have been made to be used for either feature extraction or to gather data. Here are a few of those ideas:

In a paper (Ataer-Cansizoglu et al., 2013), tracking is done by extracting points and planes from depth data and an extended prediction algorithm is used. The paper does not include details on how the actual feature detection is accomplished.

The paper (Fallon et al., 2012), introduces Kinect Monte Carlo Localization (KMCL) to calculate pose from point cloud provided by a depth sensor. KMCL uses a 3D-map of the surroundings and uses simulated depth and color images as a comparison. The KMCL requires a model of the tracked environment which differentiates it from the proposed method.

For a more detailed information on different methods, please see (Taskinen et al., 2015), a literature review on different depth related tracking methods in augmented reality. The report lists a total of 21 depth sensor related tracking and scanning articles and categorizes them by their main purpose: Localization, reconstruction or both.

2.1 Plane Filtering

Plane filtering is a way to make the tremendous amount of data a depth sensor produces a little easier to handle in computational sense. Any pixel-by-pixel method becomes very unusable when the accuracy of one pixel can vary between 1 mm to 30 mm. The problem is compounded by the fact that the data is most likely handled in 3D-coordinates. To counter this problem, the data needs to be handled in larger groups, hence the plane filtering.

The base idea is to take only a few points (samples) from data and derive possible planes from them. To actually use these planes in mesh building and tracking, a further edge detection step must be performed.

In the article (Biswas and Veloso, 2012) a Ransac based plane filtering system is proposed. In short, the plane detection is done by randomly selecting sample points to form planes and then continuing on, again

randomly, to extend that plane with additional samples. Our approach improves stability in cases where random sampling may result in unpredictable data loss. Additionally, our approach is configurable during run time, allowing a clear tradeoff between execution time and accuracy. Random selection can be tuned in similar fashion, but the resulting behaviour is not so easily predictable. One set of random points can generate more than satisfactory results for a single run, but on the next run the same number of random points can yield sub-par results. With our approach the results show a constant quality level for each grid size. This allows the fine tuning to be performed in a predictable fashion.

2.2 Simultaneous Localization and Mapping

Simultaneous Localization And Mapping (SLAM) has been originally developed for conventional color cameras but the idea can be processed with depth sensors also (Riisgaard and Blas, 2005). Closest practical example of depth SLAM would be KinectFusion (Newcombe et al., 2011), where depth sensor is used to map the data and aid the tracking in visually obscure situations like in dark spaces or colorless environments.

Real-Time mapping in SLAM has always been a problem in computer power and memory use, and in KinectFusion case the mapped model is in a memory limited cube of voxels. Other solutions have solved the memory issue by limiting the quality of the map or by using extensions to memory that may slow the computation (Whelan et al., 2012).

The part of the SLAM our method uses, does not require as much detail. This keeps the computation and memory consumption at a lower level, so it will not be an issue (See Section 5).

3 PLANE EQUATION DETECTION

This paper introduces a new method to be used with depth data to cover all the applications using multiple tracking methods with limited computing power. In terms of computing power, the plane equations are relatively easy to calculate.

Detecting planes in a depth image is simple when the right mathematical tools are being used. The three states of the proposed plane detection are illustrated in Figure 1. By using a split grid over the image, the detection task can be quantified into smaller tasks. In

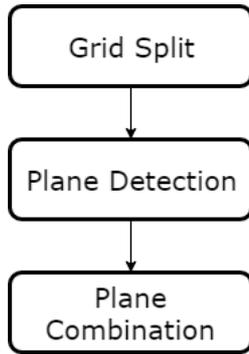


Figure 1: The three states of plane detection.

short, the grid cells will be tested for planes by using three corner points as a plane definition. The fourth corner point will then be used as a verifier for that cell. If the fourth corner point belongs to the plane, the entire cell is a plane and can be used further. It is worth noting, that it is possible to make the detection more robust by using more points in the cell to verify the plane. However, such a mechanism has not been implemented for this paper, and it remains as future work for later.

The next phase is to combine these cell planes into a larger whole. This is done by comparing cells by using the direction (normal) of the plane and one point from each plane. If they match, within an acceptable error, they will be combined into one larger plane. This task will be repeated over all the cells that have been detected as planes.

The final task is to filter useless information. All the planes that do not contain enough cell planes will be removed. For instance the corners of a room can cause plane-like data points, when the left side of the grid hits one wall, and the right side hits the other wall. Situations like this are filtered out simply by requiring that a plane must have enough supporting cells to be accepted.

Figure 2 shows the method in use. The photo is taken from a laboratory room to demonstrate the effectiveness of the algorithm in an environment where there are a lot of obstructing objects. Planes detected are named and then colored according to direction they are facing. As can be seen, planes are detected even when there are other objects creating distractions.

3.1 Notable Difference

Plane Equation Detection differs from any other technique mostly by detecting "infinite" planes. This mechanism does not directly detect physical edges of the planes as the method is mainly intended to produce features for tracking. Edges and corners can

still be detected mathematically by using plane intersections or physically by doing edge search after the equation has been found.

In Figure 2, the planes are infinite but the visible edge is a border of the group of grid cells that form a plane. This border can also be used to map the real edges when needed. Mathematically calculated edges and corners are actually used in tracking when the orientation needs to be more robust or the location needs to be tracked. The mathematical intersections provide more accuracy and stability than directly detected corners because the calculations use several points instead of just the corner. This averages out much of the noise which would affect the direct detection with full effect.

3.2 Mathematical Functions

This part describes all the mathematical functions involved in plane detection.

3.2.1 Definition of Plane

The simplest way to describe a plane is with its normal vector (\bar{v}) and one contained point (p) as illustrated in Figure 3. This plane can be transformed into linear function by using Equation 1. Planes can also be defined with two vectors instead of a normal vector. These vectors are parallel with the plane and divergent with each other. With two scalars multiplied with these vectors, any position in the plane can be generated. In this way, the calculation of plane function is faster but intersection and inclusion calculations are slower.

$$\begin{aligned} \bar{v}_x * p_x + \bar{v}_y * p_y + \bar{v}_z * p_z - \\ (\bar{v}_x * x + \bar{v}_y * y + \bar{v}_z * z) = 0 \end{aligned} \quad (1)$$

3.2.2 Plane from Three Points

A plane needs to be defined using three points of a cell rectangle. The point contained by the plane can be any of the given three points (p_1, p_2, p_3) and the direction is calculated by cross product calculation using Equation 2. If using two direction vectors is preferred, then a simple subtraction between the points will suffice (calculation without the cross product). For this paper the cross product has been chosen, because it will be beneficial in the following step.

$$\bar{v} = \frac{((p_2 - p_1) \times (p_3 - p_1))}{\|p_2 - p_1\| * \|p_3 - p_1\|} \quad (2)$$

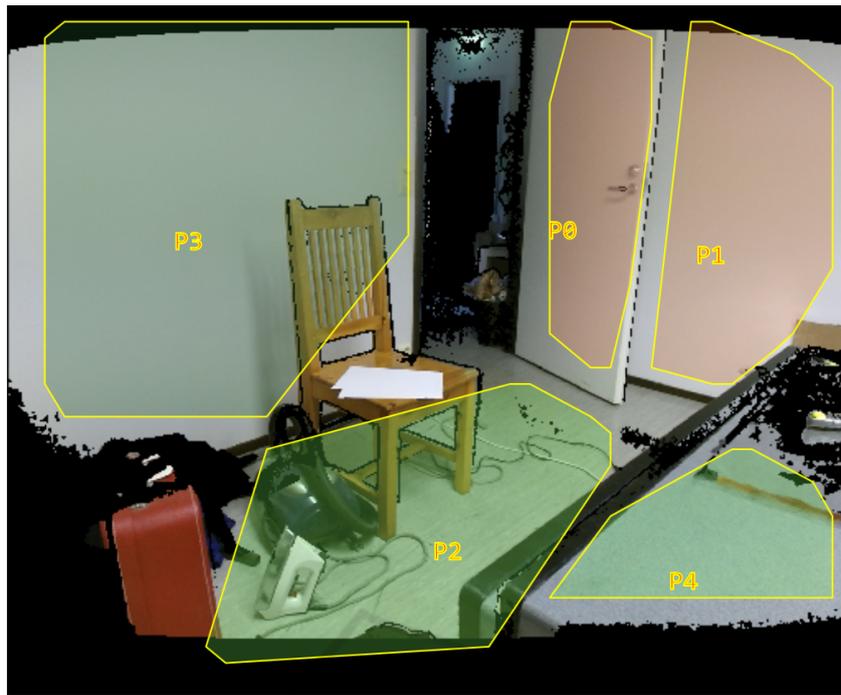


Figure 2: An image of real time feature extraction with Microsoft Kinect 2.

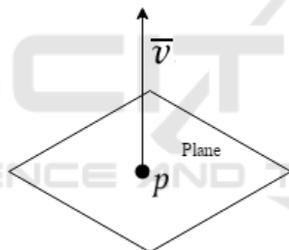


Figure 3: The definition of plane.

3.2.3 Point in Plane

Point in plane equation is used for detecting if the earlier mentioned fourth point is part of the newly defined cell plane. It is also used in plane similarity comparison in the next phase. The Equation 3, which is based on Equation 1, is used for this. This calculation requires the normal vector. When the direction vectors are being used, a cross product must be calculated to get the normal. If the cross product was already calculated in the previous step, it can be used directly without additional computations.

$$\frac{|\bar{v}_x * p_x + \bar{v}_y * p_y + \bar{v}_z * p_z - (\bar{v} * x + \bar{v} * y + \bar{v} * z)|}{\|\bar{v}\|^2} \leq \theta \quad (3)$$

In Equation 3, the θ is a threshold minimum distance of the point from the plane and it makes the equation usable with imperfect values the depth image displays.

3.2.4 Comparing Vector Direction

In order to find out, if two planes are similar, we must check if the planes have a unifying point and are facing the same direction. For the direction, a dot product is used according to Equation 4.

$$1 - \frac{\bar{v}_a \cdot \bar{v}_b}{\|\bar{v}_a\| * \|\bar{v}_b\|} \leq \theta \quad (4)$$

4 RESULTS

One way to understand the benefits of the systematic plane equation detection is to compare it with a random detection method. It does not matter what kind of random mechanism is used, as the point is to show the unreliability of any random method. In this case, the random method does predetermined amount of random hits in the image and then tries to hit three more times around the original point to get the four points necessary to test for a plane equation. The rest of the process is equivalent to the proposed plane equation method.

Another way to compare the methods is a timed benchmark where computation times are compared with different parameters. As the comparison is done between systematic and random algorithms, the results are not exact. To evaluate any random method, an iteration of many attempts is required and these

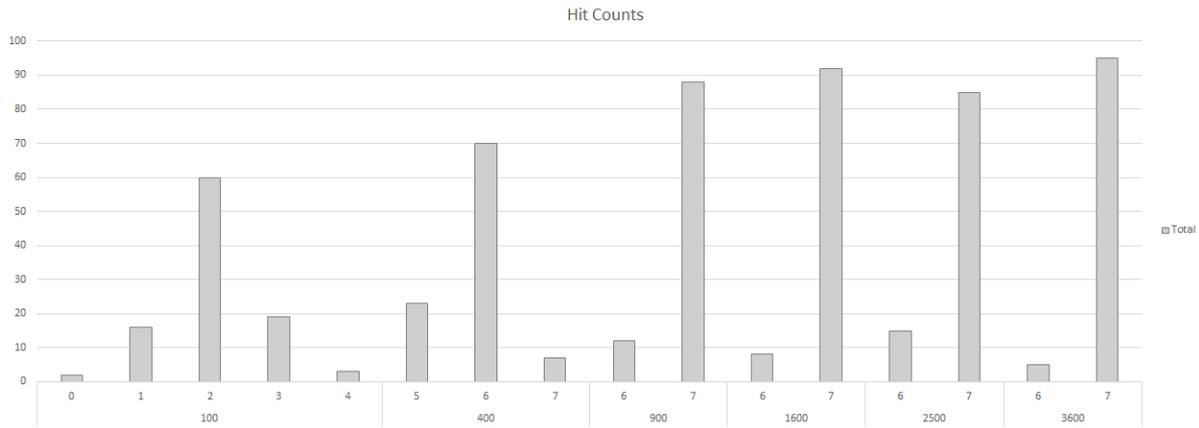


Figure 4: Distribution of plane counts for different random iteration counts.

kind of loops may be optimized at compilation or processing. Thus, unpredictable effects may occur. Therefore, the timed benchmark is still required to see if the methods are even in the same level.

Both algorithms are tested using computer generated virtual depth data illustrated in Figures 5 and 6. This provides a stable and consistent reference, unlike the real world data from a noisy sensor, which would be slightly different for each run even in the same location. Also the ground truth is known and readily available, while real world data would have to be evaluated by a human to obtain the correct value for each frame. The Figure 6 shows how many planes are detected with naked eye.

The tests have a number of parameters affecting them with similar and dissimilar parameters for each algorithm. Most of these parameters are chosen so that they produce the best possible result for both algorithms. These parameters are shown in Table 1. Field of View and Image Resolution are both based on Kinect specifications. The iterations are selected to create balance between probability testing and computing time as doing more iterations take more time and doing less result in less accurate data. The other parameter values are selected based on experiencing.

Both algorithms have one changing variable used in benchmark. For the systematic method it is the grid division and for the random method it is the point count per iteration. Figures 9 and 7 show the used values for these variables in the x-axis (for instance 40x40=1600 means 40 by 40 grid division for the systematic algorithm and 1600 points for the random algorithm). The iteration goes through same amount of plane equation tests between algorithms in each case.

The Figure 7 shows the amount of detected planes for both algorithms and also has the ground truth count for reference. The random method produces a variety of results over many iterations and the one se-



Figure 5: Depth image of ground truth.

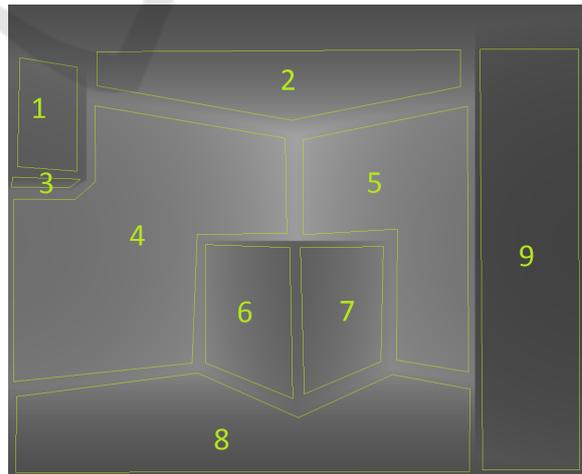


Figure 6: Ground truth with visually detected planes.

lected for Figure 7 is the most probable one selected from the overall test results shown in Figure 4. As seen in Figure 4, the results can vary when random

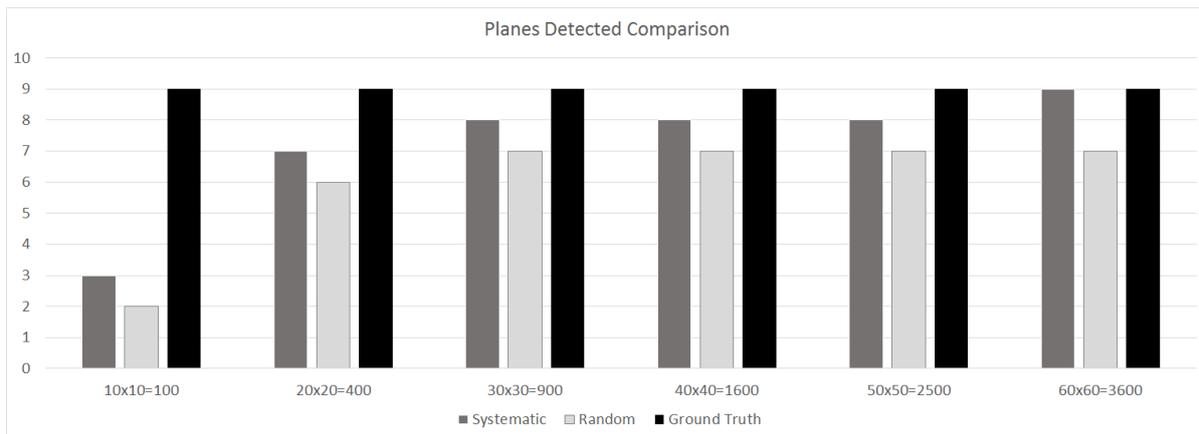


Figure 7: Comparison between random and systematic detection in detected plane count with ground truth.

Table 1: The constant parameters for benchmark.

Parameter	Value
Field of View ¹	100 °
Image Resolution ¹	512 x 424
Iterations ²	100
Maximum Radius ³	5
Minimum Plane Count ⁴	10
Minimum Radius ³	5
Normal Epsilon ⁵	0,1
Point Epsilon ⁶	0,3 [m]

¹A parameter of depth image.
²Iteration count for random algorithm.
³Distance variable for random point hits.
⁴Required number of planes in combination stage.
⁵Allowed error for direction comparison.
⁶Allowed error for point-in-plane test.

selection is being used, but as the number of iteration cycles grows, the count points more heavily towards one value.

The timed benchmark shown in Figure 9 leans strongly in favour of random detection. The difference in elapsed time between both methods is considerable but unreliable. Since the algorithms are not optimized, the optimizations in the compilation and processing phase introduce unpredictable effects to the simulation. Thus, observer affects the observed.

5 DISCUSSION

After optimization, the feature extraction can produce reliable timed benchmark results. In different stages of development, the algorithm has performed differently and in some cases could even perform fast us-

ing high quality settings (60x60 grid division). Later modifications made the library more generic and reliable in plane detection but slowed down the process. Therefore, better performance can be expected.

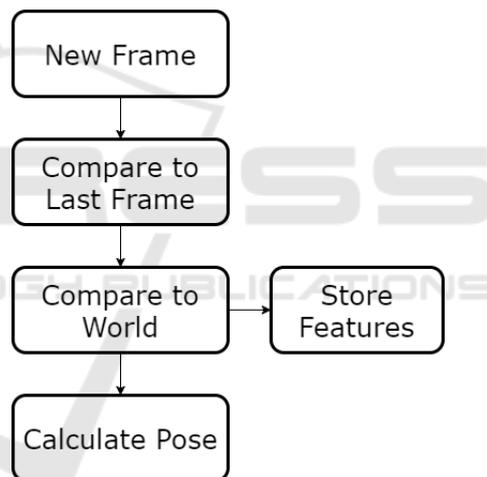


Figure 8: The flow of the tracking part.

The subject of the paper covers features for tracking but not the tracking itself. In this section we introduce an idea for tracking that can be implemented with plane equation features. The phases of the tracking are shown in Figure 8. Tracking with plane equations begins with comparing two consecutive image frames. To make the algorithm faster we can assume that the sensor won't move much between frames. That way the planes that were detected in the last frame are relatively close to the new ones. Planes that have "wandered" far can then be detected as new planes unless the entire frame has shifted to a new position. In this case we need to match at least a few combinations to get the best result of our new orientation and position (pose). We can do a fast detection run by finding the closest planes and then check them

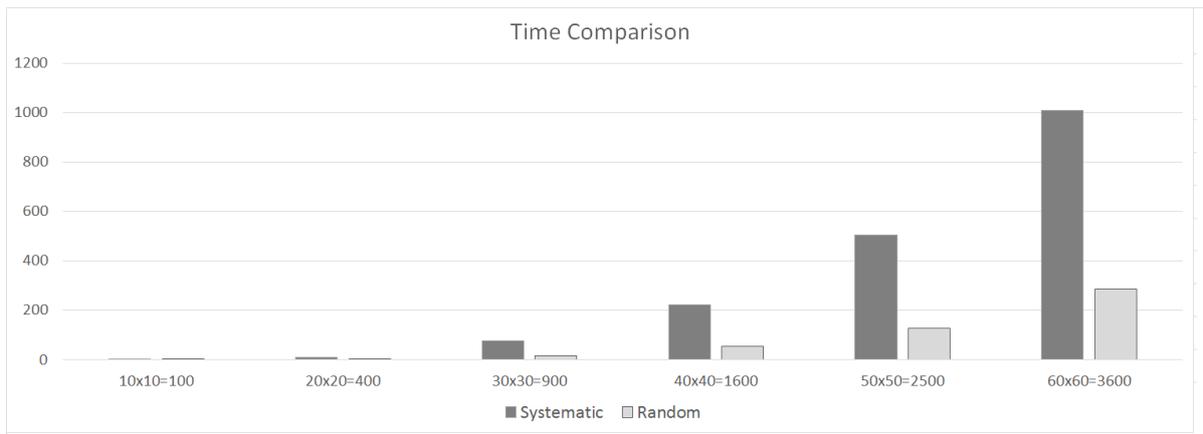


Figure 9: Comparison of execution times between random and systematic detection.

by comparing the translation values (initial guess).

When the plane matching has been done and the pose translation has been found, we can start matching our new frame with a world of planes. A world of planes is our global storage of every plane detected so far and can be used in the detection throughout the entire tracking session. Some new planes, detected between frames, might have been detected already in some earlier frame and have more precise information on pose and can aid in tracking. Constant adjustment of global plane collection is required.

6 CONCLUSIONS

We have shown that our plane detection algorithm is more reliable than random detection when detecting planes. By increasing quality (grid division), the algorithm quickly approaches the ground truth plane count. This is useful for a support algorithm as we can have desired output with low level computation. When enough planes have been detected, the information is sufficient to confirm the pose the other tracking methods have calculated.

Actual depth image is noisy and in consecutive frames there are differences in almost every pixel. In every feature extraction method, this problem is addressed by using strong features that are either an average of smaller components or have something very defining in them. Combining the data into larger planes does the same in plane equation detection, providing good tolerance towards sensor noise at a low computational effort.

ACKNOWLEDGEMENTS

The research has been carried out during the MARIN2 project (Mobile Mixed Reality Applications for Professional Use) funded by Tekes (The Finnish Funding Agency for Innovation) in collaboration with partners; Defour, Destia, Granlund, Infrakit, Integration House, Lloyd's Register, Nextfour Group, Meyer Turku, BuildingSMART Finland, Machine Technology Center Turku and Turku Science Park. The authors are from University of Turku, Finland.

REFERENCES

- Ataer-Cansizoglu, E., Taguchi, Y., Ramalingam, S., and Garaas, T. (2013). Tracking an RGB-D camera using points and planes. *Proceedings of the IEEE International Conference on Computer Vision*, pages 51–58.
- Biswas, J. and Veloso, M. (2012). Planar polygon extraction and merging from depth images. *IEEE International Conference on Intelligent Robots and Systems*, pages 3859–3864.
- Fallon, M. F., Johannsson, H., and Leonard, J. J. (2012). Efficient scene simulation for robust monte carlo localization using an RGB-D camera. *Proceedings - IEEE International Conference on Robotics and Automation*, pages 1663–1670.
- Newcombe, R. a., Izadi, S., Hilliges, D., Molyneaux, D., Kim, D., Davison, A. J., Kohi, P., Shotton, J., Hodges, S., and Fitzgibbon, A. (2011). KinectFusion : Real-Time Dense Surface Mapping and Tracking. *IEEE International Symposium on Mixed and Augmented Reality*, pages 127–136.
- Riisgaard, S. and Blas, R. (2005). Slam for dummies.
- Taskinen, M., Lahdenoja, O., Säntti, T., Jokela, S., and Lehtonen, T. (2015). Depth Sensors in Augmented Reality Solution - Literature Review.

Whelan, T., Johannsson, H., Kaess, M., Leonard, J. J., and McDonald, J. (2012). Robust Tracking for Real-Time Dense RGB-D Mapping with Kintinuous. *RSS Workshop on RGB-D: Advanced Reasoning with Depth Cameras*, page 10.

