

# Visualizing Dynamic Weighted Digraphs with Partial Links

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**Abstract:** Graphs are traditionally represented as node-link diagrams, but these typically suffer from visual clutter when they become denser, i.e. more vertices and edges are present in the data set. Partial link drawings have been introduced for node-link diagrams aiming at reducing visual clutter caused by link crossings. Although this concept was shown to perform well for some parameter settings, it has not been used for visually encoding dynamic weighted digraphs. In this paper we investigate the problem of visualizing time-varying graphs as one node-link diagram in a specific layout by exploiting the links as timelines. Partially drawn links are used to show the graph dynamics by splitting each link into as many segments as time steps have to be represented. Conventional 2D layout algorithms can be applied while simultaneously showing the evolution over time. Color-coded links represent the changing weights. We use tapered links to reduce possible overlaps at the link target nodes that would occur when using traditional arrow-based directed links. We experiment with different graph layouts and different numbers of data dimensions, i.e. number of vertices, edges, and time steps. We illustrate the usefulness of the technique in a case study investigating dynamic migration data.

## 1 INTRODUCTION

The visualization of dynamic weighted graphs is of interest in many application domains. For example, call graphs in software development, contacts among people in a social network, or protein-protein interactions in the field of bioinformatics have a relational structure which is changing over time.

Node-link diagrams are the most convenient visual metaphor to visually encode relationships among objects. The relations are graphically depicted as straight links connecting related objects, where the objects are displayed as circular, rectangular, or triangular shapes to mention the most important ones. Although node-link diagrams are intuitive representations, they typically suffer from visual clutter (Rosenholtz et al., 2005) caused by many link crossings when the graphs become denser and denser. In contrast, an adjacency matrix representation is useful for dense graphs but suffers from bad performance of path-related tasks (Ghoniem et al., 2004).

The visualization of dynamic graphs (Beck et al., 2014) makes this problem even more challenging. Using animated node-link diagrams is one solution towards solving this problem, but static displays of dynamic data benefit from preserving a viewer's mental map (Purchase et al., 2006), thus supporting com-

parison tasks and the visual exploration of such time-varying data for trends. The drawback of static diagrams is the reduced visual scalability, i.e., only a limited number of graphs of a sequence can be displayed demanding for a suitable visualization which allows graph comparisons and scales for longer graph sequences.

In this work we propose a compromise representation benefiting from the strengths of node-link diagrams as well as of static displays of dynamic graph data combined into a single graph representation which is advantageous for visual scalability. To achieve this goal we map a timeline to each directed edge which begins at the node where the edge starts and points to the target node. Each link is split into as many segments as time steps have to be displayed. The static representation also makes it easier to apply interaction techniques than in the animated case. Moreover, an additional hierarchical organization of the graph vertices can easily be attached to a static diagram.

Applying this concept to complete links soon leads to a situation where visual clutter occurs, making the diagram unreadable and useless. To mitigate this situation we apply the concept of partial links (Burch et al., 2011b; Bruckdorfer and Kaufmann, 2012), i.e., we allow the viewer to interactively

reduce the link lengths until the clutter is reduced and visual patterns can be derived. The presented approach is also dependent on the generated graph layout. We illustrate the usefulness of our technique by showing real-world graph data from people migration behavior. In this scenario we demonstrate interaction techniques implemented in the visualization tool and finally, use our technique to gain insights from such time-varying weighted relational data.

## 2 RELATED WORK

There are many application domains dealing with dynamic relational data. Consequently, related literature in this field comes in a variety of forms.

There are two camps of researchers in the field of dynamic graph visualization. Time-to-time mapping as it is used in animation is one way to show the time dependency, whereas time-to-space mapping is another way to visually depict time-varying graphs. Several comparative user studies focus on the question which of the two general visualization principles of dynamic data, in particular dynamic graph data, leads to better user performances (Archambault et al., 2011; Ghani et al., 2012; Tversky et al., 2002).

When animating a graph, a node-link diagram is generally laid out and is smoothly transformed into the sequence of layouts one after the other. This process demands for a good layout for both, each single graph in the sequence as well as for the whole sequence in order to preserve a viewers' mental map (Purchase et al., 2006) guaranteed by a high degree of dynamic stability. Offline (Diehl and Görg, 2002) and online (Frishman and Tal, 2008) approaches are investigated for their suitability to representing dynamic graphs.

Animation has some general drawbacks apart from high algorithmic complexities. The viewer can only see one graph at a time, leading to problems when comparing several graphs in the sequence to derive time-varying visual patterns and insights in the data such as trends, counter-trends, or anomalies. For this reason time-to-space mappings (Burch and Diehl, 2008; Stein et al., 2010; Brandes and Nick, 2011) have been developed which present a subsequence of the evolving graph in one view. This concept allows one to visually analyze a dynamic graph by having a look at all the graphs side by side similar to a small multiples representation (Tufte, 1983; Tufte, 1990).

One drawback of such a small multiples diagram is its poor visual scalability. For example, in the parallel edge splatting technique (Burch et al., 2011a) only one representation row is used for a graph sequence

which is already enhanced by the authors by applying the concept of Rapid Serial Visual Presentation (RSVP) (Beck et al., 2012). However, in their RSVP variant the graph sequence is animated and only one time window containing a subsequence of graphs is displayed. The parallel edge splatting idea was therefore extended to a grid-based mapping of the graph sequence while also supporting a flip-book metaphor in order to make the visualization more scalable in the time dimension (Burch and Weiskopf, 2014).

A recent article surveyed existing research in the field of dynamic graph visualization (Beck et al., 2014). The paper states the observation that today more and more static representations of dynamic graph data are designed and less animated diagrams. But negatively, the designed graph visualization typically use a small multiples representation which does not allow us to integrate the time-varying weights of the graph edges into a single static graph view.

As an enhancement in our work, instead, we do not use small multiples representations; nor do we use an animated sequence of graph diagrams. We, instead, show one graph in a convenient layout, but we additionally use each directed link as a timeline starting at the origin node. To avoid visual clutter (Rosenholtz et al., 2005) we do not draw the link completely but allow the user to interactively vary the link length similar to the originally proposed (Becker et al., 1995) and later evaluated (Rusu et al., 2011; Burch et al., 2011b) partially drawn links. Moreover, we use tapered links which do not use explicit arrow heads at the target vertices and consequently, further unclutter the node-link diagram (Holten et al., 2011). A similar concept has already been used in the TimeSpiderTrees visualization (Burch et al., 2010) in which the graph sequence is mapped to growing circles. The edges are visually encoded as straight links but only drawn partially with the goal to reduce overlaps and visual clutter.

Partial edges were mathematically modeled as a graph drawing problem (Bruckdorfer and Kaufmann, 2012) and integrated it as an interaction technique into a graph visualization tool (Burch et al., 2014). However, in their work, they did not investigate the visual encoding of dynamic weighted and directed graphs by using partially drawn links, which we illustrate in this paper.

## 3 DATA MODEL

We model a directed weighted graph mathematically as

$$G = (V, E)$$

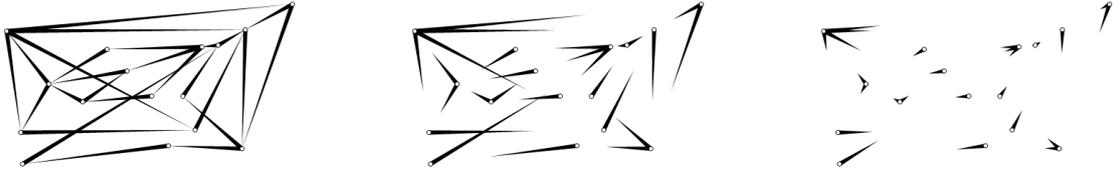


Figure 1: A directed graph containing 16 vertices and 26 edges displayed as node-link diagram using tapered links. Lengths are varied: (a) 100 % link length, (b) 60 %, (c) 20 %.

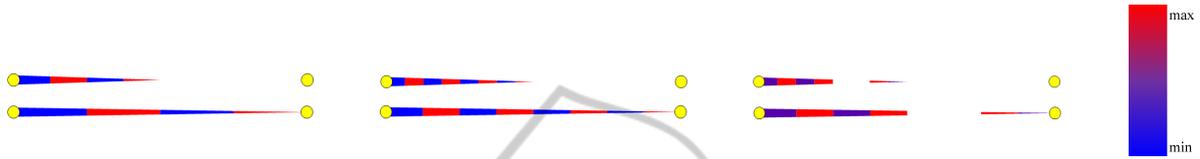


Figure 2: A dynamic weight displayed as a partial link divided into color-coded segments: (a) 4 weights and 50 percent link length. (b) 8 weights and 50 percent link length. (c) 8 time steps where at 2 of them, no edges are available, i.e. 6 weights and 50 percent link length. (d)–(f) The scenarios from (a) to (c) with 100 percent link length.

where

$$V = \{v_1, \dots, v_n\}$$

denotes the set of  $n \in \mathbb{N}$  vertices and

$$E \subseteq V \times V$$

the set of directed edges. Each edge  $e \in E$  is associated with a weight  $w(e) \in \mathbb{R}$  given by a weight function  $w : E \rightarrow \mathbb{R}$ .

In the context of this work, a layout  $L$  of a graph  $G$  is a function

$$L : G \mapsto \{(x_1, y_1), \dots, (x_n, y_n)\} \subseteq \mathbb{N}^2$$

which takes an abstract graph data set modeled as  $G$  and maps all vertices contained in  $G$  to  $(x, y)$ -positions in the two-dimensional space. In this visual encoding strategy, we follow aesthetic graph drawing criteria (Ware et al., 2002) which are responsible for making a generated node-link diagram readable, explorable, and understandable. The partial link visualization tool is implemented in the C# programming language, which supports an easy extension of the functionality by additional source code for more layout techniques.

A dynamic graph

$$\Gamma = (G_1, \dots, G_k)$$

consists of a sequence of  $k \in \mathbb{N}$  static graphs (single graphs). We define the union of all graphs as  $G_{\cup} = (V_{\cup}, E_{\cup})$  with

$$V_{\cup} = \bigcup_{i=1}^k V_i, \quad E_{\cup} = \bigcup_{i=1}^k E_i.$$

We use this union graph  $G_{\cup}$  in our visualization approach to compute a 2D layout.

## 4 VISUALIZATION TECHNIQUE

Our visualization technique is based on node-link diagrams. Each link represents a directed weighted edge and a timeline is visually encoded starting at the origin vertex and pointing to the target vertex. Color coding is used to represent the time-varying weights. We use tapered links to reduce overlaps at the target vertices when many edges point to the same vertex. Moreover, the tapered edges are perceptually useful to directly derive the edge direction (always from thicker to thinner end).

### 4.1 Partial Links

Partially drawn links have been introduced to reduce explicit link crossings in node-link diagrams. By shortening the links, the exact connections become more difficult to trace, leading to ambiguities which node is the edge's actual target node. We allow the viewer to interactively vary those link lengths until a balance between reduction of visual clutter and target node ambiguities is achieved.

Figure 1 illustrates the impact of link length reduction on the visual appearance of the node-link diagram. One can directly see how the number of link crossings is reduced but also how much more difficult it becomes to solve path-related tasks the less of the link is displayed. For example, in scenario (c), no explicit link crossings remain for the 20 percent link lengths, but it also gets harder to trace paths in the graph.

## 4.2 Time-varying Partial Links

Each graph edge is visually encoded by a straight partial link. To each of these links a timeline is attached starting at the origin vertex and pointing to the target vertex. The link is equally divided into as many segments as graphs have to be displayed. When more graphs have to be displayed as pixels on the link can be color-coded, we use a weight aggregation technique.

Figure 2 illustrates some partial link scenarios with dynamic weights in either 50 percent link lengths (a)–(c) or 100 percent link lengths (d)–(f). Here we can see that the weight is oscillating between low and high values and that at some time steps, the edge may not be available at all (c), (f).

Figure 3 illustrates how dynamic weights can be visualized in a directed dynamic graph. A planar graph without link crossings in the layout is used for illustrative purposes.

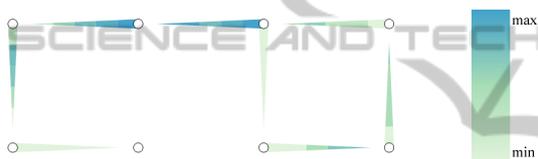


Figure 3: A small, directed planar graph with dynamic weights and the weight color mapping.

## 4.3 Interaction Techniques

Figure 4 illustrates the GUI of our visualization tool. On the left part of the GUI the user can interactively change parameters while the dynamic graph view on the right hand side is directly updated.

Apart from generating a static overview of the dynamic weighted graph data, we support an analyst by several interaction techniques to explore the data. In the following we give a short list of the most important ones of these techniques. These can be classified into techniques that allow graph layout changes, node/link/time interval selections, visual appearance changes to nodes and links, filtering techniques, and details-on-demand.

**Graph Layout.** We take the union graph  $G_{\cup}$  of the complete graph sequence into account when computing a *general graph layout*. The user can interactively decide which graph layout is applied to the graph data set. To this end we support force-directed, circular, and random layouts. After that, the user is also able to *drag and drop single nodes*. All adjacent edges are then also moved. This helps the user to make small layout changes and to see to which other nodes a

dragged node is connected because the adjacent links are smoothly moved around.

**Selection.** The user can interactively select either single nodes and links or node and link groups by clicking on them one after the other. By using rubberbanding, a connected region can be defined in which all directly selected links and the selected nodes' outgoing links are marked for link length manipulation.

**Visual Appearance.** The *diameter of nodes* and the *width of links* can be changed on demand. Tapered and traditional link representations are supported.

Showing the links all in their complete length (100 percent link length) soon leads to a situation producing vast amounts of visual clutter. The additionally attached timeline to each link makes the readability and pattern detection even worse. For this reason, the user is able to interactively and smoothly adjust the *link lengths*.

We support several *color codings* which can be selected from a given menu. The most important ones are linear optimal, vegetation, topographic, blue-to-red, or heated object color scales. Also logarithmic and double-logarithmic mappings are supported. Alpha blending can be applied on demand to *transparent links*, which is useful when these are crossing. A color gradient is used for the color coding, in which the lowest value is fully transparent and the links become more and more opaque with increasing values.

**Filtering.** Since we are dealing with weighted graphs, a user can interactively filter edges for specific *weights*. The filtered out edges are shown in gray color, i.e. they are still displayed for context information, all other edge weights are still color-coded. Also, some time periods might be uninteresting, because of a stability pattern for example. In this case, the user can filter out such *time intervals* in all of the links. The filtered out time periods can either be grayed out or removed completely from the visualization, which leaves more space for the remaining time steps. If vertices are attached with descriptions in textual form, a *text filter* can be applied. All vertices matching a given substring can either be filtered out or only those can be shown.

**Details-on-Demand.** Hovering the mouse over a node gives additional information about this node in textual form, either in a separate panel or in form of tool tips. Also the weight values can be displayed.

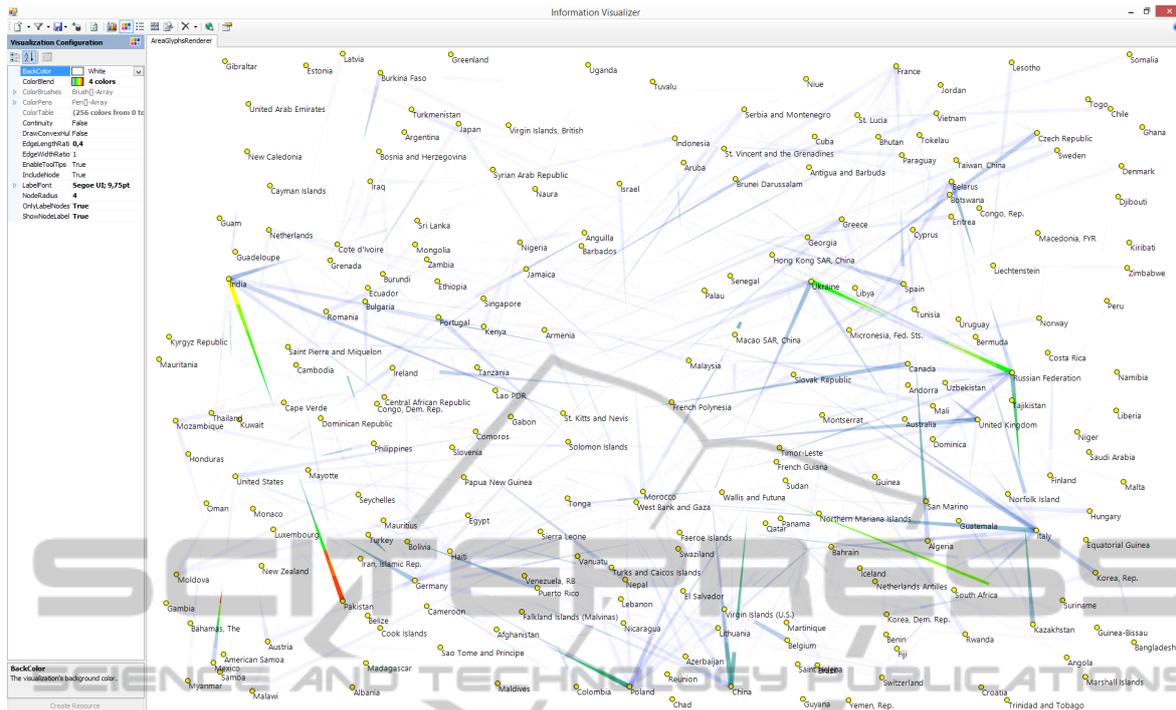


Figure 4: The graphical user interface of our visualization tool: On the left hand side the user can make parameter settings, whereas on the right hand side the currently selected dynamic weighted graph is displayed.

## 5 MIGRATION GRAPHS

In this scenario we visually explore the dynamic country-to-country migration of people in the world. The corresponding graph contains 226 vertices, 34,968 edges per time frame on average, and spans over 5 time periods (measured every 10 years between 1960–2010). The edge weights are problematic since they range from 1 to 9,367,910. Our tool can solve this by applying a logarithmic weight mapping before color coding. Moreover, to reduce visual clutter, we are able to use transparent links for the lower weight values.

Figure 5 shows the dynamic migration graph for all countries in the world over five decades. For illustrative purposes, we first generated a random graph layout, which has the benefit that the vertices are more or less equally distributed in the 2D plane. From this figure, we can draw various conclusions, of which some are illustrated below:

- **China and Hong Kong:** If we have a look at the dynamic edge pointing from China to Hong Kong, we can see that there seems to be a missing data point, i.e. for the decade from 1970 until 1980, no migration data is recorded.
- **Ukraine and Russia:** There was an increase of people migrating between Ukraine and the Rus-

sian Federation and vice versa, but after the year 2000, the number of people migrating in either direction has dramatically reduced.

- **Pakistan and India:** From 1960 to 1970, many people immigrated from Pakistan to India, but not that many in the other direction. The numbers rapidly decreased decade by decade, but still many people immigrate between both countries, which can be seen by the green colored peaks of the links pointing to each other.
- **Poland and Germany:** There is much immigration from Poland to Germany in nearly every decade, but not from Germany to Poland.
- **Mexico and United States:** The number of people immigrating from Mexico to the United States is strongly increasing, which can be seen by the red color-coded link peak.

Since we also have a hierarchical organization of the vertices (the hierarchy of the countries based on the continents, regions, etc.) we can use the geographic information to place the vertices as well (see Figure 6). The vertices in this figure are placed close to the centroid of the area representing each country. As this is probably the most familiar way of visualizing geographic positions, the viewer can readily spot the countries of interest. In this figure we use 45 per-

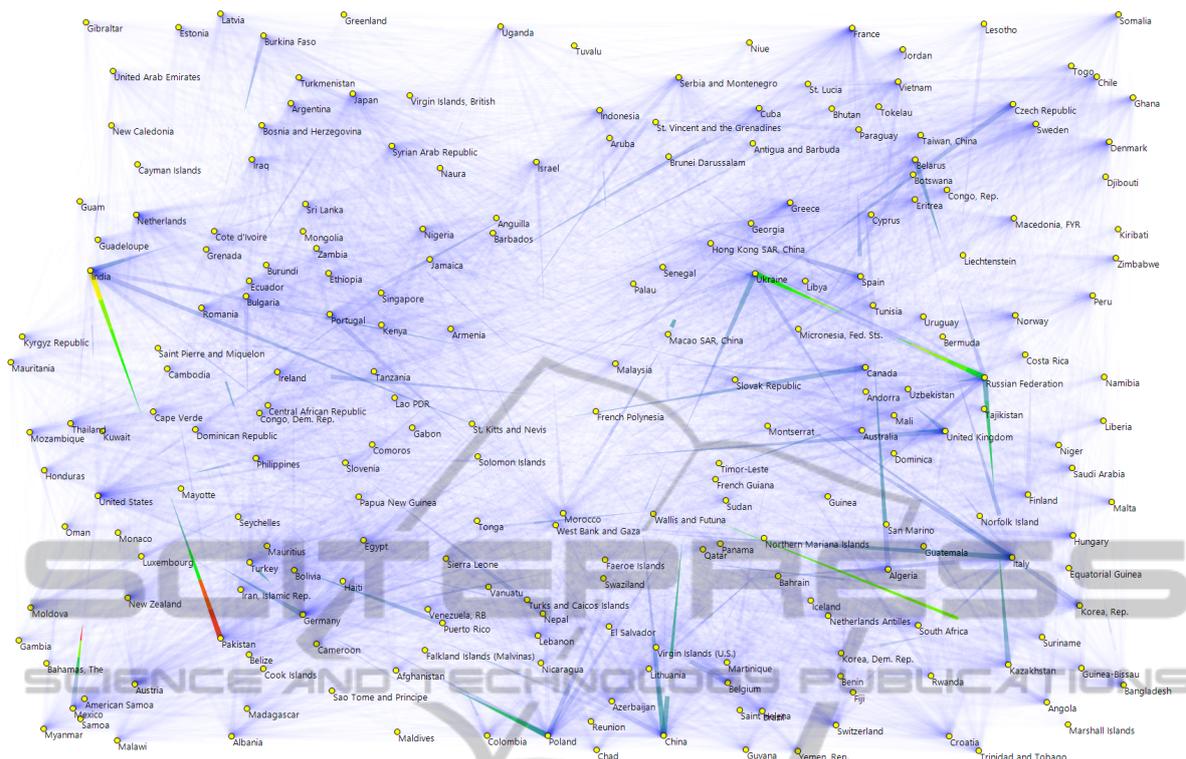


Figure 5: Migration data visualized with 40 percent link lengths and opaque color coding for low values.

cent link lengths and additionally adapt the color scale to show clearer differences to the world map in the background. Thanks to the color coding with high transparency for low migration values, we can still see differences. For example, France and Lesotho, both on the right side on the very top in figure 5, have a quite different number of target countries: For France, there are 987 outgoing edges, for Lesotho there are only 234 edges.

## 6 LIMITATIONS AND SCALABILITY

Although we designed a useful and interactive visualization technique which combines the evolution of a graph into one single graph representation in a specific layout, we are aware of the fact that there are also many limitations of our approach.

- **Layout Dependency:** The interpretation strongly depends on the layout of the graph as it is also the case for static graph visualization. Visual clutter might be reduced and graph patterns might be better perceivable if a suitable layout is generated.
- **Link Length Dependency:** The link length can be reduced, but we are aware of the fact that

if the links become too short, many more target vertex ambiguities will occur, leading to misinterpretations of the data. Moreover, differently long links (depending on the distance of two nodes) cause differently stretched timelines which may cause problems when comparing their time-varying weights.

- **Color Codings:** As with any visualization technique, the applied color coding has a strong impact on the strength of the visualization and its interpretability for visual patterns. For this reason, we leave the selection of a suitable color coding to the user, but to achieve basic expressiveness, the colors' intensities should be proportional to the encoded weight.
- **Path-related Tasks:** Our approach has benefits when solving path-related tasks since a node-link diagram is used and the dynamics of the graph is integrated into one single static diagram. Such path tracing is problematic in matrix representations, graph animations, or small multiple representations.
- **Scalability in the Time Dimension:** An increase of the number of time steps sooner or later leads to an aggregation of the color-coded weights encoded in each link which may lead to a loss of visible time-varying patterns.

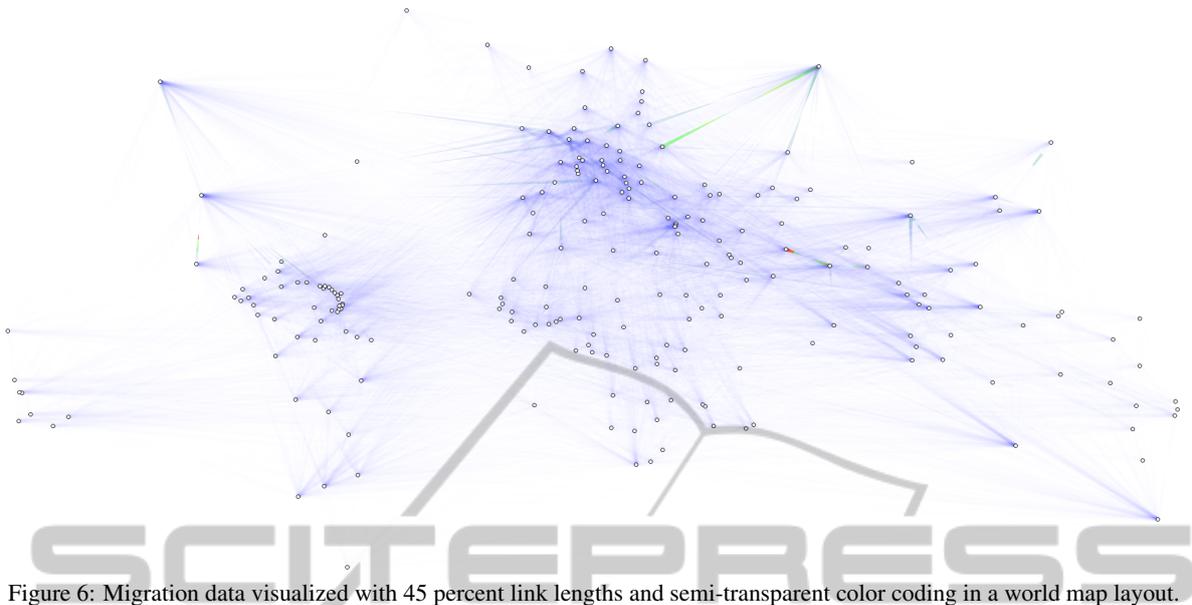


Figure 6: Migration data visualized with 45 percent link lengths and semi-transparent color coding in a world map layout.

- **Graph Planarity:** In particular, our approach is suitable for planar graphs where no link crossings occur. In such a graph scenario the question arises if we need partially links at all since those are specifically designed for minimizing visual clutter mainly caused by link crossings. But if a directed edge occurs in both directions between the same vertices, a 40 percent link length makes sense even in a planar graph layout.
- **Decreasing Thickness:** The tapered links are beneficial at the target vertices since they do not use arrow heads which would cause additional visual clutter. On the negative side, the time-dependent weights are visualized with different link thickness (large ones at the beginning and smaller ones towards the end). Whereas it is suitable for the visualization of node relations, this may cause perceptual problems when investigating edge weight variations over time (Stone, 2011).

## 7 CONCLUSION AND FUTURE WORK

In this paper we introduced a dynamic graph visualization technique which makes use of partially drawn links. The links are exploited as timelines starting at the adjacent vertices and pointing to the target vertices. The user can interactively change the link lengths in order to reduce visual clutter caused by many explicit link crossings. We experimented with

different graph layouts and illustrated our novel idea in a case study investigating dynamic migration data. We described interaction techniques and their impact on the perceived graphs, in particular on the partially drawn links.

For future work, we plan to also visually integrate an existing or computed hierarchical organization of the vertices. This is helpful to further navigate in the data and to filter it on different levels of hierarchical granularity. Our novel approach should be evaluated in a comparative user study which would give insights into the readability and usability. Also data sets from different application domains might be of interest such as dynamic social network data along with domain expert feedback for our use cases.

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