

# WaPT

## Surface Normal Estimation for Improved Template Matching in Visual Tracking

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Abstract: This paper presents an algorithm which is an improvement of the template matching technique. The main goal of the algorithm is to match 3D points with their corresponding 2D points in the images. In the presented method, each 3D point is enriched with a normal vector that approximates the orientation of the surface where the 3D point is lying. This normal improves the transfer process of patches providing more precise warped patches, because perspective deformation is taken into account. The results obtained with the proposed transfer method confirm that matching is more accurate than traditional approaches.

## 1 INTRODUCTION

Nowadays, optical tracking methods are used in many fields like robot navigation or augmented reality. In essence they establish a relationship between an internal representation of the real scene (3D point cloud) and the images which are captured by the camera. In the case of markerless tracking methods the most common solutions rely on matching some 3D points with their corresponding 2D points in each image.

Among the most used techniques are matching using feature descriptors. These techniques are robust against illumination, orientation and scale changes. However, they present some efficiency problems. For this reason while feature descriptors based methods are kept for the initial matching, other techniques, like optical flow, are used to track the 2D correspondences throughout video sequences. As optical flow estimates iteratively the displacement of each feature from frame to frame, it is prone to drift. In order to obtain more accuracy and palliate the drift in the tracking process, methods like template matching are normally used.

In these methods, for each 3D point of the point cloud a patch around its projection from a reference frame is saved as a reference template. Then template matching techniques are applied during the tracking. However, due to camera motion and the geometry of the real scene, the matching with the reference template can fail because of perspective deformations, as

can be seen in Figure 1. Nevertheless, in order to solve the mentioned problems, the reference template can be warped taking into account the camera position and the geometry of the real scene.

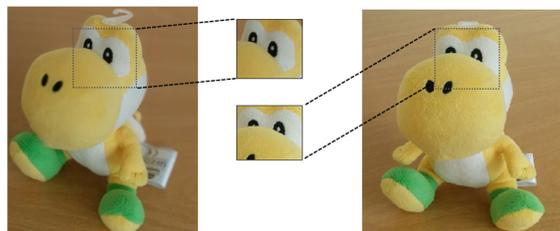


Figure 1: Perspective deformations.

This paper presents an algorithm denominated WaPT (Warped Template Patch Tracking). It improves the patch transfer process and generates a more accurate warped patch. Consequently, the template matching process is more accurate.

WaPT extends the internal representation of the real scene: each 3D point will have a normal vector that approximates the orientation of the real surface where it is placed on. In this way, the reconstruction process does not only find 3D points, but it also approximates their surface normals. WaPT uses this orientation in order to improve the template matching process.

The paper is structured as follows. Section 2 reviews related publications in visual tracking. Section

3 describes in detail the WaPT method and the underlying template transfer and matching processes. Afterwards, Section 4 shows the experiments carried on to evaluate this proposal, alongside a discussion. The paper concludes in Section 5 with conclusions and hints for future work.

## 2 RELATED WORK

Template matching techniques have been used by several authors in order to match 2D features with 3D points. Markerless tracking methods as visual SLAM (Davison, 2003) match 3D points of the reconstructed point cloud with their corresponding 2D points in the images. In order to achieve this goal, the feature detection and matching is one of the most used methods. In this way, SIFT (Lowe, 2004), FREAK (Alahi et al., 2012) and SURF (Bay et al., 2006) are very robust algorithms thanks to their invariance to illumination, scale and orientation changes. Consequently the probability of a correct match is high. However, the feature detection and matching process requires a high computational cost.

Some authors like (Barron et al., 1994) use optical flow techniques to estimate the image velocity, or the shift of a specific point from frame to frame. Although this method has lower computational cost, the estimation of the feature displacement is not as accurate as other methods and it is prone to drift.

On the other hand, relatively large image patches can serve as features. Good examples are provided by (Davison et al., 2007) and (Klein and Murray, 2007) who use patches as features. In order to match correctly these patches, they use template matching methods. The template matching processes use different operators to estimate the similarity of the patches. *Sum of absolute difference* (from now on SAD) (Watman et al., 2004) is one of them. However, in order to get better results against changes, for example brightness, there are alternatives like the cross-correlation coefficient or the normalized cross-correlation coefficient operators (Szeliski, 2010).

Template matching methods may fail to obtain the correspondences due to camera motion and perspective deformations. Surface orientation can be used in order to take into account these deformations. (Molton et al., 2004) suggest a SLAM algorithm which uses a probabilistic method to estimate the most probable surface orientation in each measurement. Later on, (Davison et al., 2007) make a simplification: they assume that 3D points always lie on a planar surface oriented to the camera where they were first seen. They assume that the appearance of

the patch will not change at all.

However, (Furukawa and Ponce, 2010) obtain very effective model reconstructions of statues and architectural elements. The work emphasizes that the use of surface orientation helped a lot to obtain such good results.

For this reason WaPT extends the approach proposing an analytic method to estimate the real orientation of the 3D point in pre-process, in order to warp the template patch better and to obtain more accuracy in the matching process.

## 3 WaPT METHOD

Based on the work by (Davison et al., 2007), 3D points are considered features that will be projected into the query images to get the localisation of the camera in real-time. In order to make this process accurately WaPT follows two main stages:

### 3D Reconstruction Stage

A 3D reconstruction of the environment is done and the estimation of a normal vector is calculated for each 3D point. This normal defines the orientation of the surface where the 3D point is placed on. This process is run off-line and the main goal is to get the point cloud of the environment and the orientation of each 3D point to make the patch transfer procedure more accurate in the next stage.

### Tracking Stage

For each input frame the following steps are done on-line:

1. Using the normal estimations calculated in the 3D Reconstruction stage the reference template is warped, i.e a fixed size patch is transferred from the current image to the reference image (where the point was first seen during the 3D reconstruction). Then, using a similarity measurement the transferred patch is located in the current image, and the center of this patch is treated as a feature.
2. Then, the vector of features obtained in the previous step is used to calculate the pose of the camera.

The following sections are devoted to describe in detail the two stages of the WaPT algorithm.

### 3.1 3D Reconstruction Stage

The objective of the 3D Reconstruction Stage (pre-process) is to generate a 3D representation of the environment. This representation should be the most

appropriate for the Tracking stage. The output of this phase is a point cloud where a normal vector is associated to each 3D point. Each 3D point lies on a surface of the environment and its associated vector approximates the surface normal. To the best of our knowledge previous work does not address the normal estimation problem and only computes the 3D points.

The point cloud is obtained using the Structure from Motion method (Dellaert et al., 2000), which will be named from now on SfM. SfM combines multi-view techniques with a Bundle Adjustment process (Triggs et al., 2000). Its input is a sequence of images of the environment. The images used in the SfM process are denominated keyFrames. The goal of our work in this paper is to estimate the normal for each 3D point of the point cloud obtained by SfM. To achieve this objective a minimization process has been designed and implemented.

Consider the case shown in Figure 2. There are two keyFrames where the same point is visible. The keyFrame where the point was first seen is denominated Reference keyframe. A normal vector is associated to the 3D point defining a plane. The figure shows the projections of the 3D point on each keyFrame. It also shows two patches around the projected 3D point and the plane defined by the 3D point and the normal.

Assume the following definitions:

**Transferred Patch.** A square patch defined around the projected 3D point in every keyFrame where the 3D point is visible, except the Reference keyFrame.

**Reference Patch.** The patch obtained when a given Transferred patch is transferred to the Reference keyFrame: the warped patch.

The process to obtain a Reference patch is the following one: given any 3D point, its projection onto the keyFrame is used to define a Transferred patch. Then, this Transferred patch is back-projected onto the plane associated to the 3D point. This new polygon is projected onto the Reference keyFrame generating the Reference patch (see Figure 2).

The objective of the minimization algorithm is to find the normal that minimizes the image difference between the two image patches.

This work uses the Levenberg-Marquardt minimization algorithm (Moré, 1978). This algorithm is an iterative process, where a random normal is taken as the initial guess. The plane defined by the normal is then used to transfer the Transferred patches to the Reference keyFrame. Afterwards the algorithm evaluates the difference between the Transferred patch and the Reference patch. The minimization algorithm adjusts the normal so that the difference between all the Transferred patches with the Reference patch is

the smallest. The algorithm exits when the difference between the last iteration and the current one does not exceed a fixed threshold.

Let us explain in detail the enumerated steps:

### 3.1.1 Feature Plane

In the projective space a plane is defined as shown in equation (1) (Hartley and Zisserman, 2003). In order to get it, three points ( $\vec{X}_1, \vec{X}_2, \vec{X}_3$ ) lying on the plane are needed.  $\vec{X}_1$  is used to represent the given 3D point. The other two points ( $\vec{X}_2$  and  $\vec{X}_3$ ) are calculated using the normal vector and the restriction imposed by equation (2), where  $(a, b, c)^T$  is the normal and  $(x, y, z)^T$  the 3D point in the euclidean space. Take into account that  $d$  is defined by equation (3). This equation presents singularities when the normal is aligned with one of the main axis.

$$\vec{\pi} = \begin{pmatrix} (\vec{X}_1 - \vec{X}_2) \times (\vec{X}_2 - \vec{X}_3) \\ -\vec{X}_3^T (\vec{X}_1 \times \vec{X}_2) \end{pmatrix} \quad (1)$$

$$ax + by + cz + d = 0 \quad (2)$$

$$d = -(ax_1 + by_1 + cz_1) \quad (3)$$

### 3.1.2 Transfer the Patch

Each pixel of the Transferred patch is back-projected onto the plane, i.e. each pixel of the Transferred patch defines a point as the intersection of its back-projected ray and the plane. Then, these points are projected to the Reference keyFrame. The process can be seen in Figure 2.

The back-projection of the point in the image is defined by equation (4), where  $P^+$  is the Moore-Penrose pseudo-inverse projection matrix of the keyFrame and  $\vec{C}$  is the center of the camera in the global reference system. In addition, a point which lies in a plane must fulfil equation (5). Solving this equation system the points are obtained. Then, the projections of these points in the Reference keyFrame are done, in order to obtain the Reference patch.

$$\vec{X} = P^+ * \vec{x} + \lambda * \vec{C} \quad (4)$$

$$\vec{\pi}^T * \vec{X} = 0 \quad (5)$$

### 3.1.3 Evaluate Difference between Patches

In order to evaluate the difference between the images of the Transferred patch and Reference patch the cross-correlation coefficient is used. The cross-correlation coefficient is a measure of similarity of

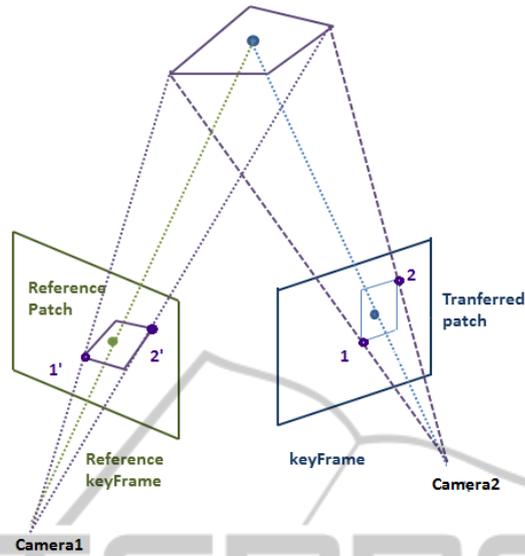


Figure 2: Transfer process: back-projection of two points from the Transferred patch onto the Reference keyFrame using a plane associated to a 3D point.

two images, where a perfect match will be 1 and a perfect mismatch will be  $-1$ . WaPT algorithm looks for the highest similarity between Reference and Transferred patches. So, the value of the cross-correlation coefficient has to be as high as possible. However, notice that this value is used in a minimization process. For this reason the objective function shown in equation (6) is used to evaluate the difference between patches, being  $crossCorrelation_i$  the normalized cross-correlation coefficient of the patch applied in frame  $i$ , and  $\alpha, \beta$  the two angles used in the parametrization of a normal.

$$\min(\alpha, \beta) \sum_i (1 - crossCorrelation_i(\alpha, \beta)) \quad (6)$$

## 3.2 Tracking Stage

As in all tracking processes the main goal of this one is to obtain the camera extrinsic parameters for each input frame. In this case the input data used for this purpose is:

1. ReferenceImage set: A set of images and their extrinsic parameters. They are the Reference keyFrames. Recall that a Reference keyFrame is where a 3D point was visible the first time in the 3D Reconstruction stage.
2. PointCloud: a set with all the 3D points that build a 3D reconstruction of the environment and their normals. This set was obtained in the 3D Reconstruction stage. Each 3D point stores the index of its Reference keyFrame in the ReferenceImage set.

The goal is to find the projections of the 3D points in the current image in order to localise the image. With this purpose,  $n$  points from the PointCloud are randomly chosen as features for the current image. Through empiric processes,  $n = 50$  has been chosen for the experiments presented in this paper. These points are projected onto the current frame. As it is assumed that the shift between frames is small the extrinsic parameters of the previous frame are used.

An adjustment has to be done in order to obtain the position of the 3D points in the current image more accurately. For each approximated projection of a 3D point we define a patch. Then, two main steps are performed to make the adjustment correctly:

1. Transfer the patch from the current image to the Reference keyFrame of the 3D point. In this way, a Reference patch is obtained.
2. A search process is performed, i.e. look for the most similar patch to the Reference patch within the current frame (similarity measurement).

### 3.2.1 Patch Transfer

The patch transfer is done using the same process as in the 3D Reconstruction stage. Firstly, the projection of the 3D point on the current image is used as the center of the Transferred patch. Using the normal of the 3D point the plane is obtained. Then, using this plane the back-projection for each Transferred patch pixel is done. The intensity of the pixel in the Reference patch is obtained using bilinear intensity interpolation. In this way, the image of the Reference patch is obtained.

### 3.2.2 Find Adjusted Projected Point

The goal of this step is to find the patch in the current image with the highest similarity to the Reference patch. With this purpose the cross-correlation coefficient is applied into an established search area. The search area is a fixed size window  $W$  within the current image. The projection of the 3D point is its center. Experimentally we found that a  $128 \times 128$  search area gives good results in  $720 \times 480$  images.

In order to achieve more accuracy in the search process a three level pyramidal reduction is applied. In this way:

- The three level reduction of  $W$  is calculated obtaining  $W_{L0}$ ,  $W_{L1}$  and  $W_{L2}$  where  $W = W_{L0}$ .
- $I$  is the original image, i.e the current image.
- In addition, a three level pyramidal reduction is also calculated for the Reference patch  $R$  obtaining  $R_{L0}$ ,  $R_{L1}$  and  $R_{L2}$  where  $R = R_{L0}$ .

Notice that  $R_{L0}$ ,  $R_{L1}$  and  $R_{L2}$  are the same image with different resolutions. In order to get robustness against noise the patches that will be used in the search process are fixed size regions placed in the center of  $R_{L0}$ ,  $R_{L1}$  and  $R_{L2}$ . Through empiric processes,  $8 \times 8$  regions have been chosen for the experiments presented in this paper.

Once the pyramidal levels are defined an iterative process is run. In this iterative process the match uses firstly the lowest pyramidal levels ( $W_{L2}$  and  $R_{L2}$ ). Then, the result is propagated to the higher levels (seen Figure 3).

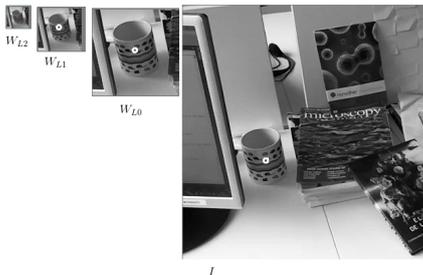


Figure 3: Iterative process where the similarity of the reference patches in different pyramidal levels is calculated. The propagation of the adjusted feature from the lowest pyramidal level to the current image can be seen as a result of the process.

So, firstly  $R_{L2}$  is found in  $W_{L2}$  using the cross-correlation coefficient and the  $8 \times 8$  region places in the center of  $R_{L2}$ . The function returns a position in  $W_{L2}$  of the region with the highest similarity to  $R_{L2}$ . This position is propagated to the next level, i.e  $W_{L1}$ . The search area of  $W_{L1}$  is redefined taking into account the position calculated in the previous step, ob-

taining  $W_{L1}'$ , which is smaller than  $W_{L1}$ . The processes are repeated and  $R_{L1}$  is found in  $W_{L1}'$ .

This iteration process is repeated until the position is propagated to the final level,  $W_{L0}$ , and finally to the original image  $I$ . In Figure 3 the propagation of the point from different levels can be seen.

This process is done for the  $n$  points, obtaining a set with  $n$  features that will be used to find the extrinsic parameters of the current camera.

## 4 EXPERIMENTAL RESULTS

This section evaluates the performance and precision of the proposed algorithm. To measure the accuracy of the algorithm, the similarity between the Reference patch and the current patch is measured. The results of our algorithm are compared to the approach employed by MonoSLAM (Davison et al., 2007), which assumes that the orientation of the 3D points always faces the camera.

With this purpose, an indoor video sequence was recorded where a camera motion around the same work place is visualized. The video sequence is built by approximately 70 frames with  $720 \times 480$  resolution.

As mentioned previously, in order to evaluate the WaPT algorithm the similarity between patches is calculated. The normalized cross-correlation coefficient is used for this purpose. The value ranges between  $[-1, 1]$ , where 1 indicates that the patches are the same and  $-1$  perfect mismatch.

In the first experiment, the similarity of the Reference patch and the current patch is calculated for  $n = 50$  points. The average of the normalized cross-correlation coefficient of all the points for each frame is calculated. Figure 4 shows the evolution of these averages during the video sequence: the WaPT algorithm is represented with a red line whereas the approach used by MonoSLAM is represented with a blue line.

The average cross-correlation coefficient value for WaPT algorithm is 0.639 and in the case of the approach used by MonoSLAM algorithm is 0.574, i.e the similarity of the patches is higher with the WaPT algorithm.

On the other hand, for each frame the median and the quartiles of the cross-correlation coefficient values are calculated. These statistics are used to measure the stability of both algorithms. Figure 5 shows the box-plots for the first 10 frames for the WaPT algorithm and Figure 6 depicts the same information for the approach used by MonoSLAM algorithm. With the aim of making the comparison visually sim-

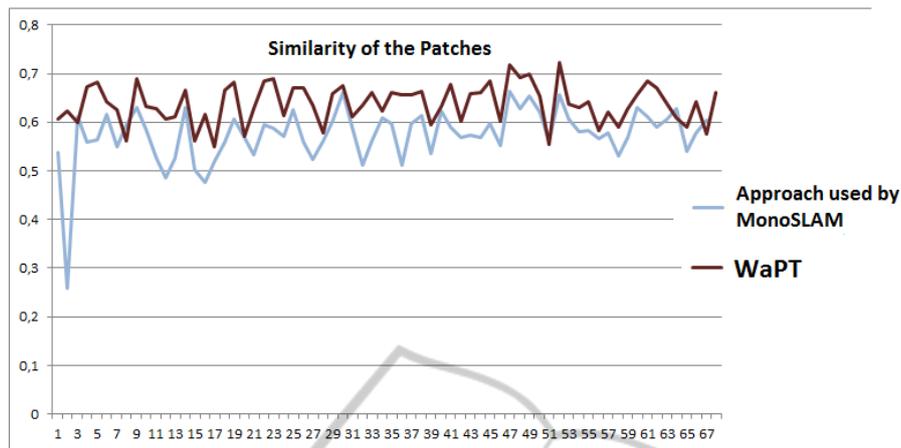


Figure 4: Evolution of the cross-correlation coefficient average values.

pler, only the first 10 frames are provided. These 10 frames are representative of the performance of the algorithms.

#### 4.1 Discussion

The first discussion point is the difference between the average normalized cross-correlation coefficient values appreciated in Figure 4. As it can be seen in the figure, the WaPT algorithm obtains higher cross-correlation coefficient values during the video sequence. These values define the similarity between images, and have to be as close as possible to 1. Therefore, applying WaPT algorithm the template matching process is more accurate due to the similarity of the patches, i.e. WaPT algorithm obtains more similar patches than approach used by MonoSLAM.

Furthermore, the average of cross-correlation coefficient values in both algorithms confirms that statement. The average value for WaPT algorithm (0.639) is 11% higher than the value obtained for the approach used by MonoSLAM (0.574). It means that taking into account that similarity is measured in range  $[-1, 1]$ , WaPT lacks a 18% to achieve a perfect match while approach used by MonoSLAM lacks a 29%.

The graphics shown in Figures 5 and 6 represent the distribution of a continuous variable (cross-correlation coefficient) for both algorithms respectively. The 3rd quartiles in the WaPT algorithm are higher than in the case of approach used by MonoSLAM.

Regarding the median values, the same trend is observed. The median values in WaPT algorithm are higher than in approach used by MonoSLAM. As a general trend, it is appreciated that the WaPT algorithm gets more similar patches than the approach

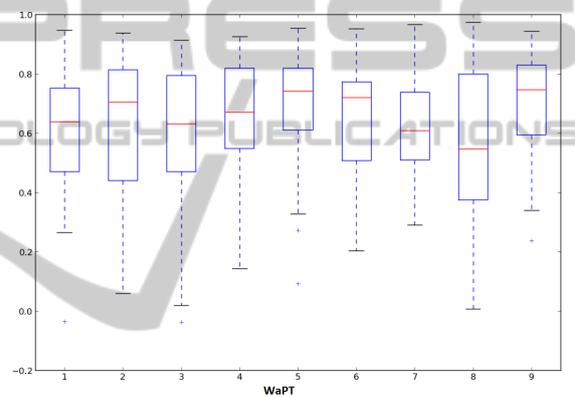


Figure 5: Box-plots of the cross-correlation coefficient values in the first 10 frames. WaPT algorithm.

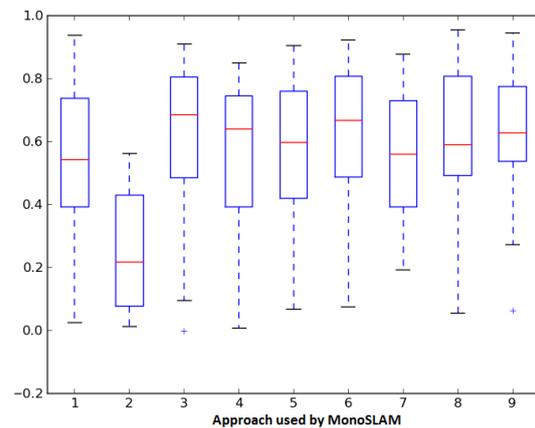


Figure 6: Box-plots of the cross-correlation coefficient values in the first 10 frames. Approach used by MonoSLAM algorithm.

used by MonoSLAM.

The box-plots graphics demonstrate it; the 3rd quartiles, the median values and even the minimum

values are higher in the case of WaPT.

All exposed data confirms that, in this test, the WaPT algorithm improves the accuracy in the template matching process, getting consequently more accurate feature positions. In autonomous navigation systems the tracking process has to be done in large environments where the data from sensors help to improve the tracking process. So, matching improvements are not critical.

Nevertheless, in augmented reality applications, the accuracy is very important to visualize the virtual elements correctly, that is, drift and jitter must be reduced as much as possible. In augmented reality applications this contribution might provide a valuable improvement. It is more accurately than template matching algorithms used in traditional methods.

## 5 CONCLUSIONS AND FUTURE WORK

The work presented in this paper proposes a new internal representation of the environment for markerless tracking. Besides the point cloud, a normal vector for each point is also stored.

In the 3D reconstruction process, not only the 3D points of the environment are calculated. A minimization process is also run in order to estimate the best normal for each point.

In the tracking process these normals are used to obtain an improved warped template in order to obtain a more precise matching.

Perspective deformations are reduced when template matching techniques and patches as features are used.

The results obtained in Section 4 are a first validation. In this validation, the similarity of the patches are calculated in order to know the matching process precision. The results have been favourable to WaPT, proving its higher accuracy. This approach provides more precision than traditional methods, which assume that the points are facing the camera.

When more experiments confirm the results provided by this paper, new research should be done in order to find methods that accelerate the reconstruction process for surface normals. One possible approach could be to start assuming that all surfaces face the camera as (Davison et al., 2007) and, on-line, perform a progressive improvement. These normals might be also useful for surface illumination compensation when comparing images taken in different lighting conditions.

As future work more validations are planned. Sequences with different perspectives, where points do

not face the camera, will be used. In this kind of sequences, the traditional methods should be even more compromised.

In WaPT, the Reference patch is located in the Reference keyFrame, which is the keyFrame where the point was first seen. In order to improve more the precision and the patch similarities, it is planned to use as the Reference keyframe the one where the point is visible and it is more similar to the current image.

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## REFERENCES

- Alahi, A., Ortiz, R., and Vandergheynst, P. (2012). Freak: Fast retina keypoint. In *Computer Vision and Pattern Recognition (CVPR), 2012 IEEE Conference on*, pages 510–517. Ieee.
- Barron, J. L., Fleet, D. J., and Beauchemin, S. S. (1994). Performance of optical flow techniques. 12:43–77.
- Bay, H., Tuytelaars, T., and Van Gool, L. (2006). Surf: Speeded up robust features. In *Computer Vision—ECCV 2006*, pages 404–417. Springer.
- Davison, A. J. (2003). Real-time simultaneous localisation and mapping with a single camera. In *Computer Vision, 2003. Proceedings. Ninth IEEE International Conference on*, pages 1403–1410. IEEE.
- Davison, A. J., Reid, I. D., Molton, N. D., and Stasse, O. (2007). Monoslam: Real-time single camera slam. In *Pattern Analysis and Machine Intelligence, IEEE Transactions on*, volume 29, pages 1052–1067. IEEE.
- Dellaert, F., Seitz, S. M., Thorpe, C. E., and Thrun, S. (2000). Structure from motion without correspondence. In *Computer Vision and Pattern Recognition, 2000. Proceedings. IEEE Conference on*, volume 2, pages 557–564. IEEE.
- Furukawa, Y. and Ponce, J. (2010). Accurate, dense, and robust multiview stereopsis. 32(8):1362–1376.
- Hartley, R. and Zisserman, A. (2003). *Multiple view geometry in computer vision*. Cambridge university press.
- Klein, G. and Murray, D. (2007). Parallel tracking and mapping for small ar workspaces. In *Mixed and Augmented Reality, 2007. ISMAR 2007. 6th IEEE and ACM International Symposium on*, pages 225–234. IEEE.
- Lowe, D. G. (2004). Distinctive image features from scale-invariant keypoints. 60:91–110.
- Molton, N., Davison, A. J., and Reid, I. (2004). Locally planar patch features for real-time structure from motion. In *BMVC*, pages 1–10.

- Moré, J. J. (1978). The levenberg-marquardt algorithm: implementation and theory. In *Numerical analysis*, pages 105–116. Springer.
- Szeliski, R. (2010). *Computer vision: algorithms and applications*. Springer.
- Triggs, B., McLauchlan, P. F., Hartley, R. I., and Fitzgibbon, A. W. (2000). Bundle adjustment: modern synthesis. In *Vision algorithms: theory and practice*, pages 298–372. Springer.
- Watman, C., Austin, D., Barnes, N., Overett, G., and Thompson, S. (2004). Fast sum of absolute differences visual landmark detector. In *Robotics and Automation, 2004. Proceedings. ICRA'04. 2004 IEEE International Conference on*, volume 5, pages 4827–4832. IEEE.

