An Approach to Simplify Navigation within Ontologies

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Abstract. Semantic Web technologies have contributed mainly to organize the knowledge and to search about this organized knowledge. One of the most complex search is to know if two entities are related within a ontology. These are called Semantic Associations, which have been classified using ρ operators: ρ -path, ρ -join and ρ -iso. Then, a ρ -query will solve any of them.

Studies about this area offer low performance execution times, but others increase the performance with pre-processing, making use of complex structures in memory. In this paper, we present semantic associations and analyze related studies. We focus on design a simplified representation of the ontology that facilitates the navigation and reduce the algorithms complexity to solve these operators, starting from the first of them: p-path.

1 Introduction

To search anything and everywhere became a common habit in the human being, but finding what it is needed is a hard work because of the information increasing. However, many tools are available in order to accomplish this task, which nowadays are based on Semantic Web technologies, i.e. using the ontology. Due to the Semantic Web, search is not only about the concepts (or entities) but also about the relationships between them, i.e. *finding how two entities are related*.

Although, ontologies (in general, Semantic Web Technologies) lead the researches to find new ways of searching, such as new visual interfaces to help the user in semantic queries [1–7] or semantic query languages (RQL [8], SquishQL [9], TRIPLE [10] and others [11–13]), the kind of search described above is not solved completely by those. Those approach need that the user knows how the resources or entities are related.

Two entities can be connected by relationships and other entities, which is why it is a complex thing, especially when these two entities are too far within the ontology. These complex relationships are called *Semantic Associations* and they have been studied and classified using the ρ operators: ρ -path, ρ -join and ρ -iso. To solve them, ontology relationships in the path between X and Y should be evaluated, and also, the entities connected by these relationships [14–17]. Therefore, this problem is about finding path problems between nodes in a graph, due to this kind of representation (the graph) is the main syntax of the ontology [9], [18–20].

Consequently, it is about retrieving the set of complete paths of the ontology graph that fits the user query in execution time, or even confirm that a path is available.

Therefore, a new approach has been developed in this paper based on a transformation of the ontology graph; which is explained in section 4. We believe that a new representation of the ontology graph will facilitate the navigation and also the algorithms to solve ρ operators.

2 The Ontology Graph

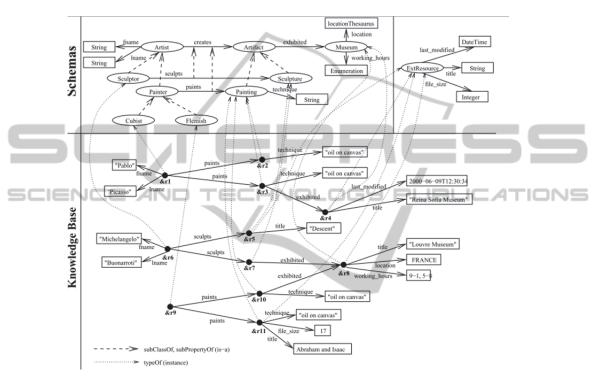


Fig. 1. Example of RDF graph.

The RDF¹ ontology can be modeled like a tagged directed graph, where triplets (Subject, Property, Object) are represented by an arc tagged with the name Property connecting the nodes Subject and Object [8], [9], [20], [21]. Therefore, the ontology navigation is about traverse the graph ontology. However, the ontology graph has to be built following the RDF definitions: Property types and classes are defined en the RDF schema (top part of Fig. 1), where a property is described by a domain (the set of classes the property applies to) and a range (the literal type or classes with values).

Classes are defined by their relationships with other classes, i.e. by the property rdfs:subclassOf, to be in the right order inside the hierarchy. Also, properties can be organized in hierarchies using the property rdfs:subproperty, and the resources are

¹Resource Description Framework is a family of World Wide Web Consortium (W3C) specifications, originally designed as a metadata data model.

defined by their relationships with other resources and by the relationship with the classes because they are instances of this classes. Then, the graph ontology built following those definitions will be very complex and the algorithms to navigate this graph will be computationally expensive [22].

Fig. 1 is an example of a part of an ontology represented by a tagged directed graph. This figure shows at the top part, the ontology schemas (two schemas in this case). At the bottom part, there is the data level or the information level, which is mostly about the instances of schema items.

2.1 Semantic Associations

The Semantic Associations were defined formally in [14], [15] based on the formal model described in [8]. In summary, semantic associations were specified using the ρ -operators described below and the ρ -query will return any of these operators:

- $\rho\text{-path}Associated$: Two entities will satisfy this property if there exists a path between them in the ontology graph, which brings from the first entity to the second entity or vice versa. For example, in Fig. 1, there is a path between resources &r6 and &r8 which represents that a sculptor Michelangelo Buonarotti has a sculpture exhibited in Louvre Museum.
- p-joinAssociated: Two entities will satisfy this property if there exists a connection node between their paths, i.e. the paths converge at some point in the graph ontology. For example, in Fig. 1, between &r6 and &r9, there is a connection point which is &r8, which represent that the artifact of this two artists (&r6 and &r9) are exhibited in the same museum.
- ρ -cpAssociated: Two entities will satisfy this property if they are descendants of the same class and they are at the same level in hierarchy. For example, in Fig. 1, &r1 and &r6 satisfy this property because they are both artists.
- ρ-isoAssociated: Two entities will satisfy this property if they have similar characteristics, i.e. their properties and classes are similar. For example, in Fig. 1, &r1 and &r6 are ρ-isomorphic, because they both represent an artist, which creates artifacts exhibited in a museum.

3 Related Work

In this section we describe some approaches that could be used to solve the ρ operators. Firstly, we describe some graph algorithms that could be applied for this and secondly, some indexing structures approaches.

3.1 Transitive Closure Computation Algorithms

Due to the graph representation of the ontology, a RDF triple (Subject, Predicate, Object) will play as a binary relation, so the computation of the transitive closure of binary relations could be applied. There are two types of approaches to cope with it:

firstly, the matrix-based direct algorithms. This approach does the computation process based on the matrix representation of graph relations.

Several algorithms are in this area, such as [23], solved by linear algebra using Gauss-Jordan and Aitkeen methods, with a O(n³) complexity, or [24], where Tarjan solved the problem of finding path expressions applied to the single source path expression problem². This study leads him to a demonstration in [25] about the mapping of this path expressions to all sorts of path problems, e.g. the shortest path search problem.

Hence, a technique that solves the single source path expression problem can be introduced and taken it as a universal solution to the problem of searching Semantic Associations as Barton proposed [16], [17], [26]. However, the Warshall algorithm [27] is the base of the matrix-based algorithms. It computes the transitive closure by traversing the matrix from the top left corner to the bottom right one.

Secondly, graph-based direct algorithms which normally work with directed acyclic graph³ (DAG). A Tarjan transformation of an arbitrary directed graph into DAG [28] could be considered to apply this approach. It is about to identify strongly connected components and replacing them with a single node (collapsing them). The base of this kind of algorithms is found in [29] where processes nodes in reverse topological order, and obtain a condensed acyclic graph. Other works [30] demonstrate how Tarjan's algorithm could be improved (in the process order).

Finally, we can find hybrid algorithms which mix two ideas above. For instance, algorithms in [31] works in two phases: First, the condensed graph is obtained by collapsing each strongly connected components, and, at the same time, the topological sort is obtained. In the second phase, the transitive closure is computed using an adjacency matrix⁴. They use an algorithm similar to the Warshall's but it is breadth-first algorithm different from those graph-based algorithms (mostly depth-first) [32].

3.2 Index Graph Traversal

The studies in [14], [15] uses a Schema Path Index (SPI) which provides fast access to all possible paths between two classes in a schema, because the ontology has the schema part relative smallest than data. However, there are paths that involve resources that belong to the data layer.

They tried to manage these situations and offer the InterClass Index (ISI). This index stores the information about the schemas that are linked due to multiple classifications (for example, in Fig. 1, &r4 has a multiple classification, because it belongs to Museum and Ext. Resource classes), but before they export the nodes at the data layer to the schema layer using artificial nodes that collapse the two class nodes.

Consequently, when a query involves resources that belong to classes (that do not have any paths between them or belong to different schemas), the ISI is searched to

²Given a graph G = (V,E) and a distinguished source vertex s, find a regular expression P(s,v) for each vertex v which represents all paths from s to v in G.

³It is a directed graph with no directed cycles, i.e. there is no way to start at some vertex v and follow a sequence of edges that eventually loops back to v again

 $^{^4}$ An n x n adjacency matrix of elements a_{ij} of a graph having n nodes is a matrix with a_{ij} having the value of 1 if there is an arc between i and j, and 0 otherwise.

find candidate nodes that if collapsed may result in a path. If no candidate node exists, an empty set is returned as a result. This idea here is finding all alternative paths that reach the terminus node from the origin node, and evaluating each one to get the final result according the ρ operator searched. To do that, they do a pre-process to store all paths between classes at the schema level in matrices. Thus, the computational complexity will be $O(|V|^{|V|})$ [32].

Another research [16], [17] propose an index of a condensed graph. The complete graph is transformed recursively to get a tree or a forest of trees, by collapsing the strongly connected components into a single node, i.e. uses the hybrid-based algorithms ideas. In each transformation, an extended signature is created to store the information about the nodes that were problematic.

They focus on the design of a new index structure and specially on solving ρ -pathAssociated and ρ -joinAssociated under the idea that searching a tree is easier than searching a graph. They based on the signature defined for trees in [33]. The information of the transformation is stored in two inverted files: one with the multiple nodes and their corresponding signatures, and the second with the signature with the list of multiple nodes. At the end, they affirm that the transforming time of the ontology into the forest of tress is about O(2n) and the creation time of the signature for each node is O(n). These times are smallest than [15].

To solve the ρ -pathAssociated, they present an algorithm that works in one direction. However the algorithm to solve ρ -joinAssociated is based on evaluating each multiple node, finding if there is a path between this multiple node and each node the origin and the terminus. Hence, this algorithm will have high computational times.

This work uses a matrix in each transformation to represent the transitive closure. Though, the final graph is smallest than the original, at the end the process of searching semantic associations have to extend recursively each component to get the original graph. Therefore, the computational time depends of the size of the matrices in each transformation. They called this approach as ρ -index [26].

4 Our Approach

The transitive closure algorithms could be applied but do not solve the problem of returning paths under certain conditions. They obtain all the paths between nodes in the original graph. That is why other approaches, although they use some of transitive closure algorithms, they create specific indexes by preprocessing the graph. This idea is the most interesting part of the related research section. Another important point will be the transformation of the graph to simplify the algorithms. Therefore, we present a transformation that will be obtained in a previous graph processing.

4.1 Transforming into a DAG

We consider approaches in [16], [17], but we follow a different idea. Instead of collapsing the strongly connected components, we make copies of the important nodes inside them, located these copies under the node on which they depend. It is

also about to obtain a forest of tree, where exits a root node and all the real nodes are dependent of it, so there will not be a recursive process.

Therefore, a node that belongs to two or more classifications, i.e. two or more classes, will be duplicated in the new graph and each copy will be located depending of the corresponding classification. As it is shown in Fig. 2, the nodes Sculpture and Painting are duplicated due to their multiple classifications, and also the node String that depends of Painting.

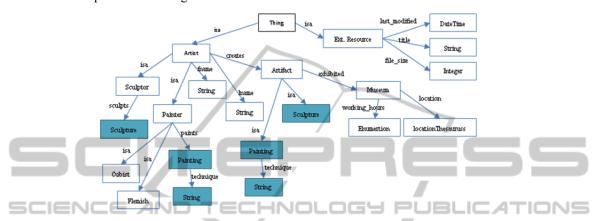


Fig. 2. Example of Transformation into DAG.

Fig. 2 is an example of a transformation of the schema part of the ontology in Fig. 1, but also, the data layer will be transformed following these ideas. The root node will be always the node Thing. Therefore, at the end we obtain one model which represents all the ontology.

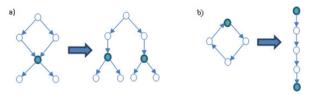


Fig. 3. Transformation of graph cycles.

We also recognize the graph cycles which maybe exist in the ontology [16], but in our case, the node will be copied many times as it is necessary to represent its dependence respect the other nodes, as it is shown in Fig. 3.

4.2 Transformation into a Numeric Representation

In the Semantic Search area, a field that involves Semantic Associations, we can find some representations, especially in complex search as [34]. They uses suffix arrays to process all the paths in the ontology graph. They use only DAG with algorithms with O(|R||E|), i.e. the resources in G. They assign number to the nodes for a quick access.

Another research [35] is based on solve the transitive of hierarchical relationships

(is-a) in KOS (Knowledge Organization Systems). One of their objectives is support the modifications of the ontology structure, because although they are less frequent, they should be solved with a minor cost. An interesting objective we share and we try to follow in our representation.

They apply a compression schema for trees which they called range compression. It is based on assign numbers to nodes according to their post-order. Then, each node will have an index that contains the minor post-order number of its descendants which with its post-order form an interval. Besides, each node will have the intervals of the nodes that can be reached and are in other tree, i.e. with a different post-order.

At the end, they increment the intervals in order to reflect the ontology modifications at minor cost. For example, the interval [1,5] will be [10,50]. This work gives us an idea of its application to semantic associations, especially to solve the ρ-pathAssociation. The intervals will be evaluating to know if two nodes are connected and the paths will be obtained easily.

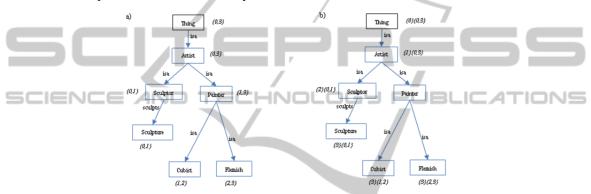


Fig. 4. Numeric representation.

Therefore, we base our work on the preceding ideas. To create our index, we traverse the graph following the preorder. So, we begin in the root node, assigning to it 0. Then, we visit the left node assigning to it the same: 0. If this node does not have descendants, the second number of the index will be the first number plus 1.

After that, we visit the right node, which will have the first number of the index equal to the second number of the left node, and its second number will be the first number plus 1 if it has not more descendants. At the end, we will visit each node twice if it has descendants and once if it has not. Finally, the root will have the second number equal to the mayor second number of its descendants.

Fig. 4a represents a part of ontology transformed in Fig. 2 with a numeric index (an interval), following the instructions we have described before. As we can observe, to solve the ρ -pathAssociation, we just could evaluate the indexes of the nodes and find if one of them is within the interval of the other, e.g., Sculpture and Artist.

However, in this representation there are many nodes with the same indexes that could lead us to confusion when nodes have to be located. Due to the necessity of a unique representation of each node, we introduce the level of dependency to the root, as it is shown in Fig. 4b. Additionally, because one of our objectives is to manage future ontology modifications with a minor cost, we will leave some space in the intervals. Therefore, if a node or several nodes are added like descendant of another

node, they could take as intervals the numbers in the space. Fig. 5 shows the new representation.

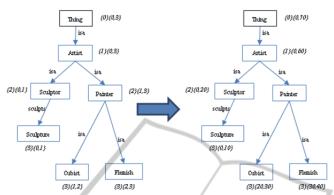


Fig. 5. Numeric Representation with space

5 Proposed Evaluation

Because this paper is only at proposal stage, in this section we will describe the experiments planned to prove it:

- Experiment 1: Comparison between preprocessing times, execution times and total times for each technique applied to one ontology. We expect to obtain the same results for each ρ -operator in each technique, but with different times. Our technique is expected to perform better than the others.
- Experiment 2: Comparison between execution times for each technique applied to different size ontologies. We expect to get a higher time with a larger ontology. We will demonstrate that our times are smallest.
- Experiment 3: Comparison between total times for each technique applied to a modified ontology. We expected that the ontology modification makes the other techniques do the whole process again. Our technique will need a little adjust.
- Experiment 4: Comparison between algorithms to calculate the space within intervals. We expected to choose the optimal algorithm to support future changes in ontology.

6 Conclusions

To solve Semantic Associations is a very complex task that needs high computational capabilities, because of the nature of the graph ontology. A transformation of this graph is presented in this paper which simplifies the navigation. This transformation is obtained by two phases: first, we transform the graph into a DAG, and second, we assign a numeric representation to each node.

The created index (i.e. the numeric representation) is based on an interval and the level of root dependence. It will facilitate the construction of algorithms regarding to

the resolution of ρ operators. An example of the procedure of one algorithm for ρ -pathAssociation is mentioned: a path between two entities is finding when one of them is within the interval of the other and with different level of dependence.

Future works will base on development the rest of the ρ operators. Besides, we need to do real experiments in a framework by implementing all the semantic associations' approaches and compare us with each of them to measure time and complexity of each technique.

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