DEPTH GRADIENT IMAGE BASED ON SILHOUETTE *A Solution for Reconstruction of Scenes in 3D Environments*

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Abstract: Greatest difficulties arise in 3D environments when we have to deal with a scene with dissimilar objects without pose restrictions and where contacts and occlusions are allowed. This work tackles the problem of correspondence and alignment of surfaces in such a kind of scenes. The method presented in this paper is based on a new representation model called Depth Gradient Image Based on Silhouette (DGI-BS) which synthesizes object surface information (through depth) and object shape information (through contour). Recognition and pose problems are efficiently solved for all objects of the scene by using a simple matching algorithm in the DGI-BS space. As a result of this the scene can be virtually reconstructed. This work is part of a robot intelligent manipulation project. The method has been successfully tested in real experimentation environments using range sensors.

1 INTRODUCTION

1.1 Statement of the Problem in a Practical Environment

The work presented in this paper is integrated in a robot-vision project where a robot has to carry out an intelligent interaction in a complex scene. The 3D vision system takes a single range image of the scene which is processed to extract information about the identity of the objects and their pose in the scene. Figure 1a) presents the real environment with the components that we are using in our work: the scene, the immobile vision sensor and the robot. In the worst case, the complexity of this scene includes: no shape-restrictions, shades, occlusion, cluttering and contact between objects. Figure 1b) shows a prototype of a scene that we have dealt with.

An intelligent interaction (grasping, pushing, touching, etc) of a robot in such a scene is a complex task which involves several and different research fields: 3D image processing, computer vision and robotics. There are three main phases in the interaction: segmentation of the scene into their constituent parts, recognition and pose of the objects and robot planning/interaction. In this paper we specifically present an efficient recognition/pose solution that allows us to know the layout of the objects in the scene. This information is essential to carry out a robot interaction in the scene. Therefore we have integrated this work as a part of the general project which is being currently used in real applications.



Figure 1: a) Robot interaction in the scene. b) Example of complex scene.

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1.2 Previous Work on Contour and Surface Based Representations

Object recognition in complex scenes is one of the current problems in the computer vision area. In a general sense, the recognition involves identifying an unknown object, which is arbitrarily posed, among a set of objects in a database. In 3D environments, recognition and positioning are two different concepts that can be separately handled when complete information of the scene is available. Nevertheless, if only a part of the object is sensed in the scene, recognition and pose appear closely related. In others words, the object is recognized through the computation of the best alignment scene-model.

As we know, there is a wide variety of solutions to recognize 3D objects. Most of them use models based on geometrical features of the objects and the solution depends on the feature matching procedure.

Among the variety of methods are those that recognize 3D objects by studying sets of 2D images of the object from different viewpoints. Some of these methods rely on extracting the relevant points of a subset of canonical views of the object (Roh, 2000; Rothwell, 1995). The main drawback of these techniques is that the detection of relevant points may be sensitive to noise, illumination changes and transformations. There are also strategies that use shape descriptors instead of relevant points of the object (Trazegnies, 2003; Xu, 2005) but most of them need the complete image of the object to solve the recognition problem.

Matching and alignment techniques based on contour representations are usually effective in 2D environments. Thus, different techniques based on: Fourier descriptors (Zahn, 1972), moment invariants (Bamieh, 1986), spline curves (Alferez, 1999), wavelets (Lee, 2000) and contour curvature (Mokhararian, 1997; Zabulis, 2005) can be found in the literature. Nevertheless, in 3D environments these techniques have serious limitations. The main restrictions are: limited object pose, viewpoint restrictions (usually reduced to one freedom degree) and occlusions not allowed. Main troubles of the contour based techniques occur due to the fact that the silhouette's information may be insufficient and ambiguous. Thus, similar silhouettes might correspond to different objects from different viewpoints. Consequently, a representation based on the object contour may be ambiguous, especially when occlusion circumstances occur. As a result, the matching problem is usually tackled by means of techniques that use surface information instead of contour information.

Surface matching algorithms solve the recognition problem using 3D sensors. In this case two different processes arise: surface correspondence and surface registration. Surface correspondence is the process that establishes which portions of two surfaces overlap. Using the surface correspondence, registration computes the transformation that aligns the two surfaces. Obviously the correspondence phase is the most interesting part of the algorithm. Recently Planitz et al. (Planitz, 2005) have published a survey about these techniques. Next, we will present a brief summary of the most important works that are closely related to ours.

Chua and Jarvis code surrounding information at a point of the surface through a feature called *Point Signature* (Ching, 1997). Point signature encodes information on a 3D contour of a point P of the surface. The contour is obtained by intersecting the surface of the object with a sphere centered on P. The information extracted consists of distances of the contour to a reference plane fixed to it. So, a parametric curve is computed for every P and it is called point signature. An index table, where each bin contains the list of indexes whose minimum and maximum point signature values are common, is used for making correspondences. The best global correspondence produces the best registration.

Johnson and Hebert (Johnson, 1999) have been working with polygonal and regular meshes to compare two objects through *Spin Image* concept. Spin image representation encodes information not for a contour but for a region around a point *P*. Two geometrical values (α,β) are defined for the points of a region and a 2D histogram is finally constructed.

In (Yamany, 2002) a representation, that stores surface curvature information from certain points, produces images called *Surface Signatures* at these points. As a result of this, a standard Euclidean distance to match objects is presented. Surface signature representation has several points in common with spin image. In this case, surface curvature information is extracted to produce 2D images called surface signature where 2D coordinates correspond to other geometrical parameters related to local curvature. *Geometric Histogram* matching (Ashbrook, 1998) is a similar method that builds another kind of 2D geometric histogram.

Zhang (Zhang, 1999) also uses 2D feature representation for regions. In this case a curvaturebased representation is carried out for arbitrary regions creating *harmonic shape images*. Model and scene representations are matched and the best local match is chosen. Adán et al. (Adán, 2004) present a new strategy for 3D objects recognition using a flexible similarity measure that can be used in partial views. Through a new curvature feature, called *Cone Curvature*, a matching process yields a coarse transformation between surfaces. Campbell and Flynn (Campbell, 2002) suggest a new local feature based technique that selects and classify the highly curved regions of the surface. These surfaces are divided up into smaller segments which define a basic unit in the surface. The registration is accomplished through consistent poses for triples of segments.

Cyr and Kimia (Cyr, 2004) measure the similarity between two views of the 3D object by a metric that measures the distance between their corresponding 2D projected shapes. Liu, et al. (Xinguo, 2003) propose the Directional Histogram Model for objects that have been completely reconstructed.

Most methods described impose some kind of restriction related to 3D sensed information or the scene itself. The main restrictions and limitations are: several views are necessary (Roh, 2000; Rothwell, 1995), isolated object or few objects in the scene, shape restrictions (Yamany, 2002; Ashbrook, 1998; Adán, 2004), points or zones of the object must be selected in advance (Johnson, 1999; Yamany, 2002; Zhang, 1999; Campbell, 2002) and occlusion is not allowed (Xinguo, 2003).

In this paper we deal with the problem of correspondence and registration of surfaces by using a new strategy that synthesizes both surface and shape information in 3D scenes without restrictions. In other words: only a view of the scene is necessary, multi-occlusion is allowed, no initial points or regions are chosen and no shape restrictions are imposed. Our technique is based on a new 3D representation called *Depth Gradient Image Based on Silhouette* (DGI-BS). Through a simple DGI-BS matching algorithm, the surface correspondence is solved and a coarse alignment is yielded.

The paper is structured as follows. DGI-BS model is presented throughout section 2 including the DGI-BS representation for occlusion cases. Section 3 presents the DGI-BS based surface correspondence algorithm and section 4 deals with correspondence verification and registration. Section 5 presents the main results achieved in our lab and finally conclusions and future work are set in section 6.

2 DGI-BS MODEL

2.1 Concept

DGI-BS model is defined on the range image of the

scene. Range image yields the 3D coordinates of the pixels corresponding to the intensity image of the scene. If the reference system is centred in the camera, the coordinate corresponding to the optic axis (usually Z axis) gives the depth information. So, the depth image is directly available.

Let us suppose a scene with only one object. Let Z be the depth image of the object from an arbitrary viewpoint v and let H be the silhouette of the object from v. Note that the silhouette H can be marked in Z.

After recording the list of pixels along the silhouette, we calculate (see Fig. 2 above), for every pixel *j* of *H*, a set of depth gradients corresponding to pixels that are in the 2D normal direction to P_j towards inside of the object. Formally

$$\nabla Z_{H\,i}^{\,j} = Z^i - Z_H^{\,j} \tag{1}$$

where

 $\forall P_j \in H, \quad j = 1, \dots, p \qquad d(P_j, P_i) = i \cdot s \quad i = 1 \dots t \tag{2}$

In expression (2), p is the number of pixels of the silhouette H, d is the Euclidean distance (in the depth image Z) between pixels P_j and P_i , and s is the distance between two samples. Note that the first pixel of H is selected at random.

Once $\nabla Z_{H,i}^{J}$ has been calculated for every point of *H*, we obtain a $t \times p$ matrix which represents the object from the viewpoint *v*. That is we have called *DGI-BS* representation from *v*.

$$DGI - BS(v) = \begin{bmatrix} \nabla Z_{H,1}^{1} & \nabla Z_{H,1}^{2} & \dots & \nabla Z_{H,1}^{p} \\ \nabla Z_{H,2}^{1} & \nabla Z_{H,2}^{2} & \dots & \nabla Z_{H,2}^{p} \\ \vdots & \vdots & \ddots & \vdots \\ \nabla Z_{H,4}^{1} & \nabla Z_{H,4}^{2} & \dots & \nabla Z_{H,4}^{p} \end{bmatrix}$$
(3)

Note that DGI-BS(v) is a small image where *j*-th column is the set of depth gradients for pixel P_j and *i*-th row stores the gradients for points that are *i*·s far from contour pixels in the corresponding normal directions. Fig. 2 (below) shows an example of DGI-BS using a colour code where black colour pixels correspond to samples that are outside the object.



Figure 2: Depth gradient concept (above). DGI-BS representation for a single view (below).



Figure 3: Viewpoints defined by the tessellated sphere and depth images synthetically generated (left). Whole BGI-BS model (right).

In practice a factor $f_{\text{mm-pixel}}$ turns $\nabla Z_{H,i}^{j}$ into pixels. $f_{\text{mm-pixel}}$ is maintained whatever scene we work with. This change makes the DGI-BS representation invariant to camera-scene distance.

2.2 The Whole DGI-BS Model

The whole DGI-BS model of an object is an image that comprises k DGI-BS representations from kdifferent viewpoints. In practice we use a synthesized high-resolution geometric model of the object to obtain the depth images. The viewpoints are defined by the nodes of a tessellated sphere that contains the model of the object. Each node N defines a viewpoint ON, O being the centre of the sphere (Fig. 3 left), from which the DGI-BS representation is generated. Thus, a whole DGI-BS model consists of an image of dimension ((k * t), 2 * p). We have duplicated dimension p in order to carry out an efficient partialwhole DGI-BS matching. Fig. 3 shows the whole DGI-BS model for one object. Note that this is a single image smaller than 1 mega pixel (1600x400 pixels in this case) that synthesizes the surface information of the complete object.

2.3 DGI-BS with Occlusion

Let us suppose that an object is occluded by others in a complex scene. In this case DGI-BS can be obtained if the silhouette corresponding to the nonoccluded part of the object is obtained in advance. We call this "*real silhouette*". Therefore, it is necessary to carry out a preliminary range image processing consisting of two phases: segmentation and real silhouettes labelling. Since this paper is focused on present the DGI-BS and due to length limitations only a brief reference of these issues is given. More details can be found in (Merchán, 2002) and (Adán, 2005).

Segmentation means that the scene splits in a set of disjointed surface portions belonging to the several objects. Segmentation can be accomplished by discovering depth discontinuity and separating set of points 3D in the range image. We have used the technique of Merchán et al. (Merchán, 2002) which is based on establishing a set of suitable data exploration directions to perform a distributed segmentation. Since this issue is not the matter of this paper, from now on we will assume that the range and the intensity image are segmented in advance.

Concerning the real silhouettes labelling, a generic silhouette H, corresponding to a segmented portion of the scene, is divided up into smaller parts which are classified as real or false silhouettes. To do that, we consider two steps:

I. Define H as a sequence of *isolated* and *connected* parts. A part is *isolated* if all their points are far enough from every other contour in the image and *connected* if it is very close to another part belonging to another contour. In conclusion, this step finds the parts of the contours that are in contact and those that are not.

II. Define *H* as a sequence of *real* (*R*) and *false* parts (*F*). The goal is to find which parts occlude to others (*R*) and which ones are occluded parts (*F*). The set of *connected* parts must be classified as real or false. Using *Z* (depth image) we compare the mean depths for each pair of associated *connected parts* (belonging to the contours *H* and *H'*) and we classify it. After comparing all *connected* pairs of *H*, the *real silhouettes* are finally obtained. See figure 4.

After carrying out the real silhouette labelling process we can obtain the DGI-BS representation for every segmented surface of the scene. In the case of an occluded object, we build DGI-BS only for the longest real silhouette of H. In practice, one or two real parts (which correspond to one and two occlusions) are expected. Of course, cases with more occlusions are possible but in any case the largest real part must be at least 30% of H. Otherwise very little information of the object would be available.

Note that in occlusions circumstances DGI-BS is a $t \times p'$ sub-matrix of the non-occluded DGI-BS version. Since a close viewpoint is available in the whole DGI-BS model, this property can be easily verified. Fig. 5 illustrates an example of this property. Now dimension p' < p but dimension t is image of the object is not complete more sampled points fall outside the object. That is why a few more number of black pixels appears in it.

3 SURFACE CORRESPONDENCE THROUGH DGI-BS

The whole DGI-BS model gives complete information of an object. Consider (O, X, Y, Z) to be a reference system O being the geometric centroid of the object, v being a viewpoint of the scene defined by the polar coordinates (ρ, θ, φ) and ϕ being the camera swing angle. When a surface portion Θ is segmented in a complex scene, DGI-BS $_{\Theta}$ can be searched in the whole model of the object. Thus, two coordinates (k_{Θ}, p_{Θ}) in the whole DGI-BS space can be determined in this matching process: the best view (index k) and the best fitting point (index p).



Figure 4: Scene C: range image processing: segmentation and real silhouettes labelling (R=Real and F=false silhouette).



Figure 5: DGI-BS representation of a non-occluded object (above) and DGI-BS representation of the same object under occlusion circumstances placed in the best matching position (below).

Now we will present the sequence of steps in the surface correspondence algorithm.

The segment is projected from camera viewpoint and the depth image Z_{Θ} and its silhouette H_{Θ} are obtained. After that, the real part of H_{Θ} is extracted according to the procedure explained in section 2.3. If there are several real parts of the silhouette the longest one is chosen and the corresponding DGI-BS_{Θ} representation is generated. Then a scene-model matching in the DGI-BS space is carried out and two coordinates in the DGI-BS space are determined.

For a database with *n* objects we have *n* candidate views, one for each object of the database, with their respective *n* associated fitting points. For every pair of index $(k, p)_m$, m=1...n, a mean square error, $e_{DGI-BS}(m)$ is defined for each candidate.

Note that the surface correspondence is based on both surface and contour information. Surface information is supplied by DGI-BS representation and contour information is intrinsic to the DGI-BS definition itself. However DGI-BS representation could be ambiguous, especially on flat surfaces and hard occlusion cases. Consequently, to make the surface correspondence algorithm more efficient, we have added extrinsic information of the silhouette. This information consists of the *Function of Angles* (FA). FA contains the tangent angle for every pixel of *real* part of the silhouette. This is a typical slope representation of a contour.

Like $e_{DGI-BS}(m)$, for every pair of index $(k, p)_m$, m=1...n, FA matching error, $e_{FA}(m)$, is calculated. Finally, by minimizing the error $e = e_{DGI-BS} \cdot e_{FA}$ the best surface correspondence is finally selected. On the other hand, a sorted list of candidates is stored for further purposes. Fig. 6 shows the best DGI-BS matching for several segments of scene C. It can be seen the DGI-BS of the best view (index k) and the DGI-BS of the segments at the fitting position (index p). The scene-model surface correspondences are shown on the right.



Figure 6: DGI-BS matching for several objects of the scene C.

4 CORRESPONDENCE VERIFICATION THROUGH REGISTRATION

Let us assume that $DGI-BS_M$ is the best candidate obtained in the correspondence phase. Note that when the DGI-BS matching problem is solved a

point to point correspondence is established in the depth images Z_{Θ} and Z_M and, consequently, the same point to point correspondence is maintained for the corresponding 3D points C_{Θ} and C_M . Thus a coarse transformation T^* between C_{Θ} and C_M is easily calculated. After that we compute a refined transformation that definitively aligns the two surfaces in a common coordinate system. Thus, through the error yielded by a registration technique, we can analyse the goodness of the coarse transformation T^* and evaluate the validity of the DGI-BS matching.

We have used the well known ICP registration technique. ICP algorithm has been widely studied since the original version (Besl, 1992) and many researchers have proposed a multitude of variants throughout the 90's (Rusinkiewicz, 2001). In this work, we have used the k-d tree algorithm and the point-to-point minimization (Horn, 1988).

The goodness of the registration and, indirectly, the recognition/pose result is validated taking into account the value of e_{ICP} . In other words, we want to establish if the candidate chosen in the correspondence phase was right or wrong.

In order to calculate a threshold value for e_{ICP} , an off-line ICP process is performed over a set of random viewpoints for all synthetic models of the database. As a result of that an e_{ICP} histogram is obtained and a normal distribution is fitted to it. Finally we define:

$$e_{\max} = ZS_{ICP} - \overline{e}_{ICP}$$
(4)

where Z is the value of the normal distribution corresponding to the 100 percentile (Z=3,99), S_{ICP} is the standard deviation and \overline{e}_{ICP} is the mean of the distribution.

After carrying out the surface correspondence and alignment phases for the best candidate, if $e_{_{ICP}} > e_{\max}$ we consider that the surface correspondence has been wrong. In this case, the next candidate in the list is taken and a new e_{ICP} is computed and evaluated again (see figure 7).



Figure 7: Correspondence verification and registration.

5 EXPERIMENTAL RESULTS

We have tested our algorithm on a set of 20 scenes captured with a *Gray Range Finder* sensor which provides coordinates (x,y,z) of the points of the scene. The depth map of the scene is obtained through the camera and sensor calibrations. Scenes are composed of several objects that are posed with no restrictions and with the same texture (Fig. 8). Dimension of the scene is 30x30 cm and the sensorscene distance is 120 cm. Our database is made up of 27 objects.



Figure 8: Some of the scenes used in our experimentation.

The values selected for the parameters to create the whole DGI-BS representation are:

- Factor $f_{\text{mm-pixel}} = 10$ pixels/cm, so depth image dimension is about 120x120 pixels. Likewise, depth images of segmented objects are converted using the same scale factor. This means that the correspondence method is independent of the object-camera distance.
- The whole representations have been obtained by using a tessellated sphere of 80 nodes (k = 80). We have also used tessellated spheres with more resolution (320 nodes) but the results do not improve meaningfully and the computational time increases a lot.
- Number of sampled pixels in the 2D normal direction t = 20 and distance in pixels between samples s = 5, so the penetration inside the depth image is 100 pixels.

Figure 9 illustrates the recognition/pose process of occluded objects in scene F. The surface portions obtained after the segmentation phase appears on the left. In this case there are three portions ①, ② and ④ that are occluded. Their corresponding depth images are shown and the real silhouettes are marked onto them. Below we present the result of the scene-model matching in the DGI-BS space for the best candidate. The best view (index k) at the best fitting position (index p) can be seen for all them. Finally, the depth image of the associated model is shown of the right. On the right we show the alignment and the spatial position of the models in the scene. We can see the 3D points of the scene and the registration result of segments. The corresponding

rendered models are superimposed onto the scene.



Figure 9: Example of surface correspondence (left) and alignment of occluded surfaces (right).

Table I shows a summary of the results for all objects of the scenes A to H. 60,5% of the objects were occluded. We have included some important information like errors in the segmentation phase ('seg. error') and noise in the range image ('noise'). A segmentation error would imply that two objects were labelled as one object or that an object was segmented in several segments. The first case corresponds to two surfaces that are joined and where there are not depth discontinuities between both surfaces. This is quite uncommon case but of course the approach would fail. The second case occurs in self-occlusion circumstances but the method works as in a single occlusion case except that the surface portions will be smaller than in nonocclusions cases. In all cases the scenes were segmented in their constituent parts achieving 100% of effectiveness. On the other hand, the noise in the range is due to shades or highlighting regions. Coordinate k, which corresponds to the best matching view, is evaluated as right (R) or erroneous (E) in the column 'view'. This is a visual evaluation that report us the total percentage of failures in the DGI-BS matching phase. In our experimentation we obtained 2,6 % of failures in this phase (1/38).

The column labelled 'candidate' means the first candidate of the list that verifies $e_{ICP} < e_{max}$ and that finally is chosen as candidate. In 63,2 % of the cases the first candidate was the first of the list and the average position was 2. Finally, the last column gives information about the ICP algorithm itself showing the number of iterations in the ICP algorithm. In summary we can conclude that the approach is highly effective (97,4%).

Figure 10 shows examples of pose for multioccluded objects (scenes E, F and H) and the complete reconstruction of the scenes A, B and G.





Figure 10: Example of recognition and pose of multioccluded objects (above) and rendered representation of the complete scene (below).

6 CONCLUSIONS

This work deals with the problem of correspondence and registration of surfaces by using a strategy that synthesizes both surface and shape information in 3D scenes with occlusions. The method provides at the same time recognition and pose of segments of the scene. This work is part of a robot intelligent manipulation project.

DGI-BS (Depth Gradient Image Based on Silhouette) representation is a complete and discrete representation suitable in 3D environments. Moreover, DGI-BS representation can be applied to obtain a complete model as well as a partial model of an object. This property allows us to use it in complex scenes with multi-occlusion.

Recognitions and pose problems are solved by using a simple matching algorithm in the DGI-BS

space that yields a coarse transformation. Afterwards, registration is sorted out by computing ICP alignment of corresponded surfaces.

We are currently working on the detection and correction of wrong correspondences. Part of these problems may be due to noise and errors in 3D data acquisition stages.

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