

# A Multi-Resolution Learning Approach to Tracking Concept Drift and Recurrent Concepts

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**Abstract.** This paper presents a multiple-window algorithm that combines a novel evidence based forgetting method with data prediction to handle different types of concept drift and recurrent concepts. We describe the reasoning behind the algorithm and we compare the performance with the FLORA algorithm on three different problems: the STAGGER concepts problem, a recurrent concept problem and a video surveillance problem.

## 1 Introduction

Incremental learning is used more and more often today across many domains. The reason for the increased focus on incremental learning techniques is that the learning is dynamic and hence it is more applicable to real world situations such as on-line processing or mining large datasets. An important issue of incremental learning which this work addresses is that of tracking and adapting to changes in the data, specifically we refer to the problem of concept drift. A brief definition of the problem of concept drift is as follows: *“In many real-world domains, the context in which some concepts of interest depend may change, resulting in more or less abrupt and radical changes in the definition of the target concept. The change in the target concept is known as **concept drift**”* [8]. The main difficulty in tracking concept drift is that there is no prior knowledge of the type, pace and timing of the change that is likely to occur. Hence model based or time series based approaches are not suited for this problem.

A crucial aspect of the concept drift problem is forgetting. The algorithms developed to handle concept drift generally use a time based mechanism to control the forgetting process which generally leads to two problems: useful information is being discarded and the system converges more slowly to the target concept. Furthermore, the systems simply react to changes rather than attempt to predict and classify the changes in the data.

This paper presents a multiple window approach to track different types of concept drift. The algorithm attempts to interpret current data as well as detect, predict and quickly adapt to future changes in the concept. The system is designed to work in an on-line scenario where the data consists of a sequential stream of examples which are used by the system to derive a concept description that is consistent with the information observed.

The work presented makes three novel contributions. The first novel aspect of the research is that the algorithm uses a usefulness based approach to control the forgetting

mechanism used to discard data from the system's memory. Rather than using a time based approach, the forgetting mechanism analyses the newly observed data instance to determine how well it fits with the rest of the instances in the system's memory and the current concept definition. Based on the the rest of the data, the mechanism also determines if the new instance is a likely indicator of a change in the concept. Once the usefulness of the instance has been estimated, the system checks both the usefulness and age of the instance to determine whether or not the the instance is to be discarded. The second contribution is that the algorithm predicts the rate of change to give the system a pro-active approach to the data and thus improve the accuracy of the concept tracking. The algorithm consistently checks the current rate of change and estimates (based on past history) what the future rate of change is likely to be. This information is used to improve the control over the size of the larger dynamic data window which acts as the memory of the system and it allows for a faster adaptation to changes in the concept. The third contribution is the representation used for the concepts tracked. Rather than storing a simple generalization of the data observed, we represent the concept through a combination of instance generalizations, data predictors and the rate of change observed when concept was stable. Moreover, we use a knowledge repository to store old concept descriptions to avoid having to "re-learn" recurrent concepts.

## 2 Related Work

The issue of concept drift has been investigated for many years and several systems have been developed to address the problem of concept drift. The aim of the research in this area is to develop algorithms that will allow a system to adapt concepts quickly to permanent change while avoiding any unnecessary changes if the change observed is determined to be virtual (temporal) or noise.

The first system developed to deal with concept drift was STAGGER [7]. The learning method employed by STAGGER is based on a concept representation which uses symbolic characterizations that have a sufficiency and a necessity weight associated with them. As the system processes the data instances, it either adjusts the weights associated with the characterizations or it creates new ones.

The FLORA family of algorithms implements a moving window approach to deal with concept drift [9, 2]. FLORA2 is a supervised incremental learning system that uses a stream of positive and negative examples to track concepts that change over time. FLORA2 has a heuristic routine to dynamically adjust its window size and uses a better generalization technique to integrate the knowledge extracted from the examples observed. FLORA2 has been improved first by adding new routines to better handle noise (FLORA3) and to handle the issue of recurring contexts (FLORA4).

A different approach to dealing with concept drift was used in the AQ-PM [5] and SPLICE [1] batch learning systems. AQ-PM is a partial memory system, [5, 6, 4]. The system analyzes the training instances and selects only "*extreme examples*" which it deems to lie at the extremities of concept descriptions. SPLICE [1] is an off-line meta-learning system that uses contextual clustering to deal with concept drift that occurs as a result of hidden changes in contexts. The learning process assumes that some con-

sistency exists in the data and the system groups together sequences of instances into intervals if the instances appear to belong to the same concept.

### 3 Motivation for new approach

Algorithms developed to deal with drift implement some type of moving window that acts as the system's memory. The instances in the memory are used to track and update a target concept. As the window moves over data observed, new instances are added to the memory while the oldest instances are discarded. Instances once forgotten cannot be recalled. The aim is for the algorithms to adapt quickly to the changes observed in the data while still being robust to noise or virtual drift [9]. If a true change is detected in the data, the system should remove all old and irrelevant information from the memory and update the concept description to keep it consistent with the data observed. If the change detected is just noise or virtual drift then the system should not make any changes to the concept description and should remove all the misleading data instances from the memory. Hence tracking concept drift accurately depends on the capacity of the system to make the correct decision when discarding information from the system's memory. *If the system either discards instances which are still relevant or keeps instances that are no longer useful then its tracking will be severely affected.*

To deal with this problem most algorithms use a time-based forgetting mechanism where an instance ages over time as more new instances are observed. There are three problems with this approach. The first is the assumption that the oldest instances in the window are less relevant and hence should be the first to be removed from the window. The second problem is that all data instances stored in the window have equal importance in the processing involved on the target concept. These two assumptions are not correct especially in applications where the data contains random noise or involves some virtual change in the concept. For example, consider the case where the data instances observed have been consistent for a period of time but the last few instances have been affected by random noise. Using a simple time based forgetting approach, older but noise free instances would be discarded from the memory while the newer but noise affected instances would be kept which would be incorrect. Furthermore, as all instances would be considered to be of equal importance, then the most recent noise affected instances would affect the target concept definition as changes would be made to keep the definition consistent with the data observed.

Another major problem with most existing algorithms that track drift is that they lack a mechanism for predicting and estimating future data changes. Prediction is very important for two reasons. First, it can be used to control the size of the system's memory. Different types of change have different requirements in terms of forgetting. If the change involved is abrupt, then the size of the memory needs to be reduced by a large margin to allow the system to adapt faster to the changes. However, if no change is detected, then the size of the memory can be increased to allow for a more accurate description of the target concept. If the system has a good estimate of the rate of change, then it can reduce/increase the memory size accordingly. Second, prediction can be used as a cross-validation tool on past decisions to discard data and modify the memory size. This is particularly important for the approach described in this paper as

the instances are not removed from all windows at the same time (the larger window keeps data instances for a longer time interval). If the change is predicted correctly, then subsequent data instances will provide confirmation in the form of more accurate tracking and possibly fewer changes made to the memory size. The following section covers a number of basic definitions that are used through the remainder of the paper and describes in detail the forgetting and prediction mechanisms developed to address the problems outlined above. The section also includes the description of the overall tracking algorithm. Finally, current algorithms store only generalizations of the data observed in the window and generally lack the capacity to handle recurrent concepts. This is a significant drawback as the system has to “re-learn” recurrent concept definitions (but were forgotten when the concepts changed) and thus its tracking accuracy is badly affected.

## 4 Multiple Window Approach with Relevance Based Forgetting and Prediction Analysis

### 4.1 Preliminaries

The different types of concept drift can be defined in terms of two factors: *consistency* and *persistence*. *Consistency* refers to the change that occurs between consecutive instances of the target concept.

Let  $\theta_t$  be the concept at time  $t$  where  $t$  is  $0, 1, 2, 3, \dots, n$  and let  $\epsilon_t = \theta_t - \theta_{t-1}$  be the change in the target concept from time  $t-1$  to  $t$ . A concept is considered to be *consistent* if and only if  $\epsilon_t \leq \epsilon_c$ , where  $\epsilon_c$  is termed the *consistency threshold*. Let the size of the window which represents the system’s memory be  $X$ . A concept is considered to be *persistent* if and only if  $\epsilon_{t-p}, \epsilon_{t-p+1}, \dots, \epsilon_t \leq \epsilon_c$  and  $p \geq \frac{X}{2}$ , where  $p$  represents the *persistence of the change* (the interval length of consecutive observations over which the change is consistent). If the change observed in the target concept is both *consistent* and *persistent* then the drift is considered to be *permanent*. If the change is *consistent* but *not persistent* then the drift is considered to be *virtual*. Finally, if the change observed is *neither consistent or persistent* then the drift is considered to be *noise*.

### 4.2 The Evidence Based Forgetting Module

To address the problems associated with the time based forgetting approach outlined in section 3, a new evidence based forgetting method has been developed. The idea behind the approach is that an instance needs to be stored in the window if and only if there is evidence that justifies its presence. The evidence can come in two forms. First, an instance is relevant to the target concept and the rest of the data observed. Second, an instance is a likely indicator of a change in the concept. Hence if an instance has no evidence justifying its inclusion in the system’s memory, regardless of its “age”, then it should be discarded. Each instance stored in the moving window is assigned three values: *an evidence value, an age value and a change indicator value*. All three values are updated each time a new instance is added to the window. The *age value (age)* is derived by checking its position in the system’s memory. The older the instance the

higher the age of the instance. The *evidence value* ( $ev$ ) of the instance is determined by how well the instance matches the current target concept description and the other instances stored in the system's memory. The better the match the higher the evidence value. The *change indicator value* ( $\Delta$ ) depends on the evidence value. In some cases a newly observed instance may not match either the target concept or the rest of the instances in the system's memory. In this case the instance is flagged as a potential indicator that a change is about to occur in the target concept and hence its removal from the window will be delayed. The delay is user defined.

This type of forgetting offers several advantages. First, the instances are discarded from the memory based on how useful they are to the target concept and the data observed rather than based only on their age. Second, it helps the system to identify quickly the forgetting point  $\phi$  in the data (the instance which indicates the start of permanent drift in the target concept). As all instances have a *change indicator value*, the system only needs to find the instance that has the highest value to find the forgetting point. Furthermore, the evidence values can be used to help determine the type of drift in the concept. This is because the drift is reflected in the way in which the evidence value varies over time. Consider the following example. Let  $\theta_t$  be the concept tracked at time  $t$  and data instances stored in the memory at time  $t$  be denoted by  $I_1, I_2, I_3, \dots, I_n$ . Also let the new instance to be added to the memory be denoted by  $I_{n+1}$ .

If the instance  $I_{n+1}$  is the start of *permanent drift* in the concept, then the evidence value  $ev$  assigned to the instance will be low as the instance does not match well  $\theta_t$ . Similarly the age value  $age$  will also be low as the instance has just been added to the window. However, the change indicator value  $\Delta$  will be high making  $I_{n+1}$  a potential candidate for the forgetting point in the data. Because of the persistent change in the concept, as more data is observed, the newly observed instances will match  $I_{n+1}$ , thus incrementing both its  $ev$  and  $\Delta$  values while the older instances seen before  $I_{n+1}$  have their  $ev$  values decremented. Also as more new instances that match  $I_{n+1}$  are added to the window and old ones are discarded, the concept definition changes and becomes a better match for  $I_{n+1}$  thus further incrementing its  $ev$  value. If the instance  $I_{n+1}$  is the start of *virtual drift* in the concept or is just *noise*, then both the  $ev$  and  $age$  values assigned to the instance will be low (the instance is new but does not match well  $\theta_t$ ) while the  $\Delta$  value will be high making  $I_{n+1}$  a potential candidate for the forgetting point in the data. However, as more data is processed, the  $ev$  and  $\Delta$  values have a different behaviour when compared to the reinforcement seen when dealing with *permanent drift*. *Virtual drift* does have *consistency* but lacks *persistence*. Hence the  $ev$  and  $\Delta$  values for instance  $I_{n+1}$  are incremented only for a short interval of time. As soon as the data reverts back, the instance  $I_{n+1}$  will not longer match the most recently observed data. Therefore its  $ev$  and  $\Delta$  values will be decremented and the instance will quickly be discarded from the window. If instance  $I_{n+1}$  is only *noise* then it is unlikely to match any of the subsequent instances since noise has neither *consistency* nor *persistence*. Hence, both its  $ev$  and  $\Delta$  values will be decremented as more data is processed and the instance will be forgotten as soon as the user predefined delay expires.

### 4.3 The Prediction Analysis Module

To improve the tracking performance of the algorithm, a prediction component was added. The original competing windows algorithm (CWA) [3] on which this work is based, used an estimate of the change in the concept to handle drift in the target concept  $\theta_t$ . This approach has been modified to allow the system to predict the future rate of change  $\epsilon_t$ .

The rate of change  $\epsilon_t$  prediction involves the analysis of the short term history of the change observed in the target concept. If the history indicates that the rate of change has been consistent then the predicted rate of change is the average of the past  $\epsilon_t$ . However, if the rate of change has not been consistent, then the prediction is derived based on the short term trend of past  $\epsilon_t$  and the difference between the predicted  $\epsilon_t$  and the actual  $\epsilon_t$ . Hence, if the trend shows an increasing rate of change and the true rate is still larger than the predicted rate, then future predicted values are increased. The analysis of  $\epsilon_t$  is used to control the size of the system's memory. If the actual  $\epsilon_t$  is significantly larger than the predicted  $\epsilon_t$ , then the size of the current window is too large, and it needs to be reduced. This in turn is used to remove more instances with low evidence value in the window. However, if the predicted  $\epsilon_t$  is larger, then the window size can be increased and it may not be necessary to forget any of the instances currently in the memory.

### 4.4 Algorithm Description (MRL)

Overall the algorithm attempts to detect and track changes in the target concept using a multi-resolution approach. The algorithm uses two windows which compete to produce the best interpretation of the data. The reason for using multiple windows is that in order to deal with all types of drift, more than one interpretation of the data is needed. Furthermore, the use of two windows allows a more gradual forgetting as data discarded from the smaller of the two windows is not discarded from the larger window. The concept tracked, as mentioned in the introduction, is represented by a combination of instance generalizations, data predictors and the rate of change observed when concept was stable. Both the instance generalization and the data predictors are in essence partial instances that describe the common characteristics of the data observed in the window.

The main body of the algorithm is shown in Figure 4.4 while the forgetting and prediction components are shown in Figures 4.4 and 4.4 respectively. The notations used are as follows:  $\theta_t$  is the concept tracked at time  $t$ ,  $l^c(w)$  is the length of the window  $w$ ,  $\epsilon_c(w)$  is the rate of change in window  $w$ ,  $\Psi$  is the forget set.

The processing done by the algorithm is outlined below. Initially, after the average of the data vectors in the window has been computed, the number of observations over which the change is consistent is set to 1. Then for each subsequent data sample observed, the system attempts to determine the rate of change. To do this, the concept definition for each of the two windows is updated at each step  $t$  using the formula  $\bar{x}_t(w) = 1/|w| \sum_{i=0}^{|w|-1} x_{t-i}$ . This newly derived concept definition is then used to compute the change in the window. The change is obtained by subtracting the concept value in the window at time  $t-1$  from the concept value in the window at time  $t$ . The current change is then compared with the consistency threshold. If the current change in the window is smaller than or equal to the consistency threshold  $\epsilon_c$ , then the persistence value for the

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Begin
For each time  $t$ :
  For each window  $w \in \{S, M\}$ :
    Increase  $|w|++$  if not already at maximum size
    Compute the change  $\epsilon_t(w)$ 
    /* Update the persistence value for the window */
    If  $|\epsilon_t(w)| > \epsilon_c$  then
      Reset the persistence for the window  $p(w) = 1$ 
      Update consistent change  $\epsilon_c(w) = \epsilon_t(w)$ 
    Else
      /* Increment persistence value for the window */
       $p(w)++$ 
    Call Do-Forgetting;
    Call Do-Prediction;
    /* Resetting smaller window */
    If reset-flag = true
      Remove all instances before  $\phi$  in  $w$ 
      Store concept  $\theta_t(w^*)$  in repository
    Empty  $\Psi$  for small window
    /* Resetting larger window */
    If  $p(w) = 2|w|$  then
      Set the next larger window size to  $2|w|$ 
    Else If reset-flag = true
      Remove all instances before  $\phi$  in  $w$ 
      Store concept  $\theta_t(w^*)$  in repository
    Empty  $\Psi$  for medium window
    /* Compute estimated concept */
    If  $w$  is reset then
      Recompute  $\bar{x}_t(w)$  and  $\epsilon_t(w)$ 
      Set concept  $\theta_t(w) = \bar{x}_t(w)$ 
    Else
      Set concept  $\theta_t(w) = \theta_{t-1}(w) + \epsilon_c(w)$ 
    /* Return the concept from best window */
    Best window  $w^* = \arg \max_w(w)$ 
    Return  $\theta_t(w^*)$ 
End

```

Fig. 1. The main algorithm.

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Do-Forgetting;
For each window  $w \in \{S, M\}$ :
  /* Determine the instance relevance */
  For each instance  $I$  in current  $w$ 
    Increment  $age$ 
    For each instance  $J$  in current  $w$ 
      If Match( $I, J$ )
        Increment  $ev$  and  $\Delta$  of  $I$ 
      Else
        Decrement  $ev$  and  $\Delta$  of  $I$ 
        /* Reset the forgetting point */
        If  $\Delta$  of  $I$  is largest observed
           $\phi = I$ 
    /* If instance has low relevance or
    instance has high age
    then add it to the forget set */
    If  $ev$  and  $\Delta < 0$  OR  $age < \text{max-age}$ 
      Add  $I$  to  $\Psi$ 

```

Fig. 2. The Forgetting Module

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Do-Prediction;
For each window  $w \in \{S, M\}$ :
  /* Do rate of change prediction */
  Check  $p(w)++$ 
  If  $\epsilon_t$  consistent
    predicted  $\epsilon_t = \bar{\epsilon}_t$ 
  /* If the rate of change is inconsistent
  compute a new estimate and
  check repository for recurrent
  concepts */
  Else
    Rate-Difference =  $|\text{predicted } \epsilon_t - \epsilon_t|$ 
    Check  $\epsilon_t$  Trend
    Check-Repository
    For  $i = 0$  to  $\frac{w}{2}$ 
      Compute predicted  $\epsilon_t$ 
      reset-flag = true;

```

Fig. 3. The Prediction Module

window  $p$ , is incremented by one. Else the persistence value for the window is reset to 1.

The algorithm then proceeds to analyse the data samples stored in the window to determine their usefulness as well as to identify possible forgetting points ( $\phi$ ). Each instance in the window is matched first against the current concept definition and then against the other instances in the window. For each match found, the evidence value  $ev$  of the instance is incremented. Furthermore, if the instance is likely to be a change indicator, for each match the  $\Delta$  value is also incremented. However, if a mismatch is found then the  $ev$  and  $\Delta$  values are decremented. The instance that has the largest  $\Delta$  value is considered to be the new forget point  $\phi$ . When all instances in the window have been processed, the algorithm selects those with very low  $ev$  and  $\Delta$  values as well as high age values and adds them to the forget set ( $\Psi$ ).

The algorithm also checks the predicted rate of change. If the rate of change is consistent then the predicted rate for the next  $\frac{w}{2}$  time steps is set to the mean of the rate

of change observed in the past. However, if the rate of change is not consistent, then the difference between the predicted and actual rate of change is computed. Next, the algorithm checks the repository for old concept descriptions that may match the newly seen data. If a match is found, then the concept is reset to the old definition. The trend of the change observed is analysed and used to compute a new set of predicted values for the next  $\frac{w}{2}$  time steps. The reset flag is also set to indicate the size of the window should be reduced if the true rate of change is greater than the predicted rate.

Next, the algorithm deletes the instances in  $\Psi$  and makes changes to the window size if required. If the reset flag is set to true then all instances observed before the forget point are discarded from the window and the size of the window is reduced. However, the size of the larger window can also be reset as a result of the consistency observed in the smaller window. If the change in the small window is persistent for more than  $2S$  observations, then enough consistency has been found in the small window and the medium window is reset. When the medium window is reset, its size is reduced from  $M$  to  $2S$ . At any time instance, a concept has a description in each of the 2 windows, and a degree of persistence for the concept in that window. The best concept definition is given by the description of the largest sized window that has longest consistency.

The algorithms requires that two parameters be set by the user. The first parameter defines the length of the history to be used when analysing the trend of the change in the concept. The algorithm uses as default a value of  $\frac{w}{2}$  for the processing which experiments done have indicated to be sufficient to generate good estimates. The second parameter defines the delay used to prevent the removal of instances that have low usefulness but are likely indicators of change in the concept. The default value for the delay was set at  $\frac{w}{3}$  but in noisy domains a shorter delay may be more effective.

## 5 Results

The algorithm was applied to two problems that involve concept drift. The first was the STAGGER concepts problem which is the standard benchmark used to test concept drift tracking algorithms. The second problem involved the interpretation of an average frame extracted from video surveillance.

### 5.1 STAGGER Scenario

The STAGGER concepts scenario is described in detail in [7] and involves a dataset of 120 instances divided into 3 stages. The target concept changes at an interval of 40 instances. The aim is to track the concept with the highest possible accuracy while adapting to the changes observed in the data. The experiment was run 100 times and the average accuracy of the system is shown in Figures 4 (noise free data) and 5 (data contained 20% noise). The results from using FLORA on the same data are also shown for comparison purposes. The reason for selecting FLORA is because it uses the most popular form of tracking drift with a single dynamic window and it implements heuristics routines to adjust the window size based on the changes detected in the data. The results show that the algorithm presented in this paper tracks the concept with high

accuracy and adapts very quickly to the changes in the data. The performance of the algorithm decreases as more noise is added to the data both in terms of tracking accuracy and speed with which it converges to the target concept. However, when compared with FLORA, the new algorithm's performance is better in all three cases and in particular it adapts faster to the changes in the data.

## 5.2 Recurrent Concept Scenario

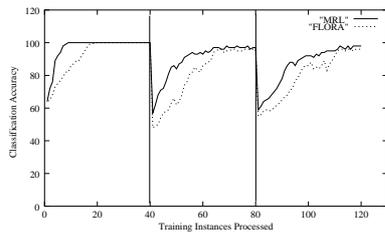
The second experiment used to test the algorithm involved tracking a recurrent concept. The scenario involved a modified version of the STAGGER concept problem. In this case we added a fourth stage of 40 instances. The concept from the first 40 instances was repeated in the third stage of the experiment. The concept from the second stage was repeated in the fourth stage of the experiment. The success was measured by how well the system handled the repeated concept. The experiment was run 100 times and the average accuracy of the system is shown in Figures 6 (noise free data) and 7 (data contained 20% noise). The results show that the system adapted significantly faster to the target concept when the concept was repeated. FLORA is also able to recognise past concepts but its accuracy is slightly lower due to its reliance on instance based concept generalizations.

## 5.3 Background Frame Problem

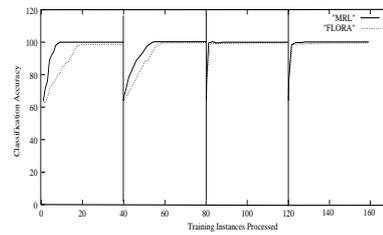
The third experiment involved tracking changes in the average frame computed from video surveillance. A simple way to detect motion in surveillance is to analyse the differences between a preset video frame and the frames obtained from the live surveillance. The problem is that in many cases, gradual changes in the background due to changes in the environment conditions (such as faulty flashing neon-lights) are interpreted as actual motion which results in a large number of false alarms. The dataset used for this problem contained 300 video frames from a stationary camera as shown in Figure 8. The lighting conditions change four times over the 300 frames. The aim for this problem was to track the changes in the average frame as accurately as possible. The results are shown in Figure 9. The plot shows the true concept value over the 300 instances as well the concept value derived by the drift tracking algorithm. Overall, the accuracy of the algorithm is very good and there is little delay before the concept is adapted to the changes in the data.

## 6 Conclusions

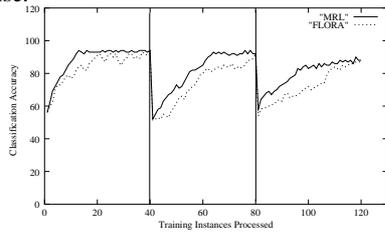
This paper describes a multiple window algorithm that combines evidence based forgetting and prediction analysis to track concept drift. The work presented makes two novel contributions: it introduces a new mechanism for forgetting and it uses a prediction method to control the size of the windows and thus allow a more pro-active interpretation of the data. The algorithm was tested using two datasets: the STAGGER concepts problem and a background frame tracking problem. The results obtained show that the algorithm adapts very quickly to changes in the data and tracks drift with very good accuracy.



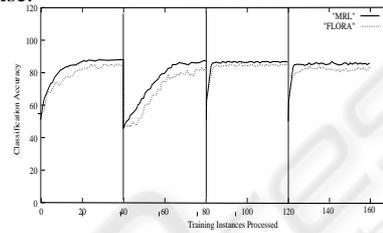
**Fig. 4.** Classification results of data without noise.



**Fig. 6.** Classification results of data without noise.



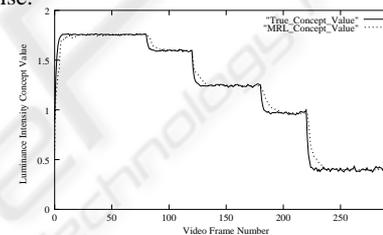
**Fig. 5.** Classification results of data with 20% noise.



**Fig. 7.** Classification results of data with 20% noise.



**Fig. 8.** Surveillance Image.



**Fig. 9.** Classification results for background frame problem.

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