Hybrid Strategy for Automatic Stellar Classification

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Abstract. This paper describes an hybrid approach to the unattended classification of optical spectra of stars. The classification of stars in the standard MK system constitutes an important problem in the Astrophysics area, since it helps to carry out proper stellar evolution studies. Manual methods, based on the visual study of stellar spectra, have been frequently and successfully used by researchers for many years, but they are no longer viable because of the spectacular advance of the objects collection technologies, which gather a huge amount of spectral data in a relatively short time. We therefore propose a cooperative system that is capable of classifying stars automatically and efficiently, by applying to each spectrum the most appropriate method or combined methods, which guarantees a reliable, consistent and adapted classification. Our final objective is the integration of several artificial intelligence techniques in a unique hybrid system.

1 Introduction

Spectroscopy is among the most powerful currently available techniques for the study of stars and, in particular, their physical conditions (temperature, pressure, density, etc.) and chemical components (H, He, Ca, K, etc.). In general terms, a stellar spectrum consists of a black body continuum light distribution, distorted by the interstellar absorption and reemission of light, and by the presence of absorption lines, emission lines and molecular bands [1].

The stellar spectra are collected from telescopes with appropriate spectrographs and detectors. Observers collect the flux distribution of each object and reduce these data to obtain a one-dimensional spectrum calibrated in energy flux (erg-1cms-2s-1Å-1) and wavelength (Å). The study of the distribution of spectral types and the analysis of spectral data can help to understand the temporary change of the physical conditions of stars from a statistical point of view, and therefore, to learn about their evolution. This is why spectral classification is one of the fundamental aspects of the evolutionary study of stars, and a phase that must be carried out in a fast, efficient and accurate way. This work is part of a global project devoted to the study of the last phases of stellar evolution. As part of our project, we have collected a large sample of optical stellar spectra from astronomical observations carried out at several telescopes. In order to extract useful information from the collected spectra, we must complete a solid and systematic classification in the current Morgan-Keenan system (MK).

The MK classification system was firstly proposed in 1943 by Morgan, Keenan & Kellman and has experienced many revisions ever since [2]. This classification system quantifies stellar temperatures and levels of luminosity. Stars are divided into groups, i.e. spectral types, that are mainly based on the strength of the hydrogen absorption lines and on the presence or absence of some significant lines of Ca, He, Fe, and molecular bands.

The temperature of the stars is divided in a sequence called OBAFGKM, ranging from the hottest (type O) to the coolest (type M) stars. These spectral types are further subdivided by a decimal system, ranging from 0 (hottest) to 9.5 (coolest). In addition, a luminosity class (from I to V) is assigned to the star, which depends on the intrinsic stellar brightness. That is, the hottest star of the MK system would be of spectral type O0 and the coldest would be a M9 star.

This two-dimensional system is the only one that is widely used for stellar classification. One of its main advantages is that MK classifications are often static, because they are based on the visual study of the spectra and on a set of standard criteria. However, the same spectra can be classified differently by different experts and even differently by the same person at different times.

The estimation of the spectral type and luminosity of stars is often carried out by human experts, who analyze the spectra by hand, with no more help than their own experience. The manual classification techniques are often based on the visual study of the spectra and on a set of standard criteria [1]. These manual analyses usually lead to a MK classification of the spectra.

Although the manual methods of classification have been used successfully for many years, they are no longer viable, since the current collection technologies allow us to obtain a huge amount of spectral data in a relatively short time. The manual classification of all the spectra that are currently available would involve a considerable increase in time and human resources; it is therefore highly advisable to optimize the manual procedure by means of automatic, fast and efficient computational techniques.

Our main objective is to formalize a hybrid system that is able to determine the most appropriate classification method for each spectrum type and to obtain on-line MK classifications through an Internet Stellar Database (http://starmind.tic.udc.es).

The following sections start by describing the spectral data that were used to design and test the automatic classification techniques. Secondly, we describe the morphological analysis algorithms that were applied to the spectra before presenting them to the automatic techniques. Finally, we present the different artificial intelligence models that were implemented and we contrast their results.

2 Spectral Data

We have chosen a complete and consistent set of 258 spectra that cover all the types and luminosities of the MK system, in order to design the artificial models that will be applied to the classification problem. This set is sufficiently representative because it offers a continuous transition of the spectral features between each spectral type and its adjacent types. The selected spectra were previously analyzed and corrected by human experts who collaborate in the project. We have used the public catalogues of Silva [3] - 28 spectra sampled in the range of 3500 to 8900 Å with 5 Å of spectral resolution -, Pickles [4] - 97 spectra sampled in the range of 1150 to 25000 Å with 5 Å of spectral resolution -, and Jacoby [5], 133 spectra sampled in the range of 3510 to 7426 Å with 1.4 Å of spectral resolution.

In order to guarantee the generalization of the designed and implemented models, we have built the training or design set with approximately 50% of the spectra of each spectral type, leaving around 15% for validation and the remaining 35% to evaluate the classification capability of each model.

Before presenting the spectra to the automatic techniques, we carry out a morphological analysis of all the spectra in order to obtain the values of the parameters that characterize each spectrum separately.

3 Morphological Analysis

The patterns that are presented to the selected models were obtained automatically by means of signal processing techniques that measure the spectral peculiarities (absorption and emission lines, spectral energy, molecular bands, etc.).

In particular, we measure the 25 spectral features that can be grouped into three general types:

- Absorption and emission lines: including hydrogen, helium and metallic lines (Ca, K, Fe, etc.).
- Molecular bands: hydrogen and carbon absorption bands.

- Rates between lines: CH-K rates, He-H rates, etc.

The signal processing algorithms used to obtain the spectral parameters are mainly based on the spectral continuum estimation and the energy measurement. Although the details of morphological analysis are out of the scope of this paper, it is necessary to mention that it is not a trivial task since spectra are affected by the interstellar reddening and by the noise that measurement instruments generate.

From a morphological point of view, an absorption line is a descending (ascending for emission) deep peak that appears in an established wavelength zone. To accurately calculate the intensity of each line, we carry out an estimation of the local spectral continuum. We smoothen the signal with a low pass filter, excluding the peaks in an interval around the sample where the line was detected. This filter is implemented by a five-point moving average method that selects the five more stable fluxes. That is

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$$C_{j} = \left(\frac{\sum\limits_{j=n}^{j+n} E_{i} * X_{i}}{N}\right), \qquad (1)$$

where C_j is the estimation of the continuum for sample *j*, E_i is the flux in sample *i*, N is the number of values used in the moving average method to calculate the local spectral continuum, and X is a binary vector that indicates the representative fluxes of the spectral continuum in the zone. This means that $X_i = 1$ if E_i is a flux value representative of the local spectral continuum, and $X_i = 0$ if E_i is a peak. The intensity is positive for the absorption lines and negative for the emission lines.

A molecular band is a spectral zone where the flux suddenly decreases from the local continuum during a wide lambda interval. For the molecular bands this means that we only have to measure their energy to decide if they are significant enough. In this case, the upper threshold line for each band is calculated by means of linear interpolation between the fluxes in the limits of the interval defined for each band. The area between this line and the axis of abscissas is then calculated with a discrete integral, and the area that surrounds each band is calculated by integrating the flux signal between the extremes of the band. Finally, the flux of the band is obtained by subtracting both calculated energies. That is

$$B_{ir} = \int_{1}^{r} L(\lambda_i) - \int_{1}^{r} E(\lambda_i), \qquad (2)$$

where *Blr* is the flux of the band between the samples *l* and *r*, *L* is the projection line, *E* is the flux function, λ the wavelength, *l* the left limit of the band and *r* the right limit. Since the obtained value becomes more negative as the band becomes deeper and wider, positive or negative values close to zero are not considered as bands.

The artificial intelligent techniques of this experimentation have been designed and tested so as to consider both the described spectral parameters and full spectral data as input patterns.

4 Classification Methods

Among the existing techniques of artificial intelligence, Knowledge-based Systems (KBS) and artificial neural networks (ANN) seem to be most appropriate to approach the problem of stellar classification. Knowledge-based systems can reproduce the reasoning of experts in order to classify spectra; neural networks are capable of learning the intrinsic relations of the patterns with witch they were trained. We have also implemented clustering algorithms to perform a sensibility analysis of the input spectra, although this technique is not currently used to obtain MK classifications of stars.

Our main objective is to integrate all the designed and implemented techniques in a unique hybrid system capable of applying the best classification method to each input

spectrum. The developed system includes two different tools: a spectral analyzer and a stellar classifier.

The spectral analyzer makes an exhaustive morphological analysis of the spectra, using the described algorithms to obtain a numerical parameterisation. It is developed in Builder C++ and integrates ad hoc ActiveX components for the visualization of spectra.

The analyzer retrieves the spectral data from a relational database that stores and structures the information from human and bibliographic sources. At present, approximately 400 spectra of our survey are stored in the database, and they will be soon available via the Internet.

The stellar classifier is based on the development of the different artificial models that were chosen to approach the MK classification of stars. We used both the spectral parameters obtained by the spectral analyzer and the full spectral data to build the input patterns of the artificial intelligence techniques. The neural networks were implemented with the Stuttgart Neural Network Simulator [6], the clustering algorithms were developed with MATLAB v.6.5.1 [7], and the expert systems were implemented in OPS/R2 [8].

At present we are developing a web site that will make the stellar classifier available through the Internet. Our main purpose is to allow users world-wide to classify their stellar spectra on-line in a fast, efficient and comfortable way.

After analyzing the performance of each technique separately, we implemented the best models in C^{++} by integrating them with the spectral analyzer, which provides us with a unique tool for the processing and classification of the optical spectra of stars.

The next sections describe the different models that are integrated into the stellar spectral classifier.

4.1 Knowledge-based Systems

This first approach proposes the implementation of a knowledge-based system that combines signal processing, production rules and fuzzy techniques, obtaining a very satisfactory emulation of the current manual process.

As a previous step towards the design of the expert systems, we carried out a sensibility analysis of the classification parameters (absorption lines, molecular bands, etc.). As a final result, we have defined as many fuzzy variables as classification levels (global, type and subtype) for each luminosity class; we have also defined the fuzzy sets and membership functions determined by the values of the spectral features in the guiding catalogue spectra.

The developed knowledge-based system stores the information that is necessary to initiate the reasoning process in the facts base. This descriptive knowledge of the spectra is represented by means of frames, i.e. objects and properties structured by levels. This model was chosen because it is the simplest and most adequate to transfer the analysis data to the classification module and allows us to establish the equivalence between analysis data and knowledge. The knowledge of the facts base includes general information, such as the names of the stars, and the results of the morphological analysis, i.e. the values of the classification parameters.

The real parameters of spectral classification and the limit values of each type and subtype were included in the expert system in the shape of fuzzy rules. The rules base

is that part of the system where the human classification criteria are reproduced. We have adopted IF-THEN production rules for the implementation of this module, because they allow us to manage the uncertainty and imprecision that characterize human reasoning in this field.

The conditions of these rules refer to the values of the parameters stored in the current facts base (working memory). The conclusions allude to three levels of spectral classification: global (late, intermediate, early), spectral type and luminosity, and as such, the module communicates actively with the facts base.

To decide what rule to apply at each moment, we used the Means-End Analysis strategy (MEA) [9]: basically, among the rules that were incorporated last into the working memory, this strategy chooses the not executed rule that has the largest number of patterns. The production rules are linked in a forward reasoning, guided by objectives. The strategy used for the reasoning process combines guided reasoning methods with a method based on truth values. The rules also have associated credibility factors that were obtained from interviews with experts and from the bibliography of this field.

We used the Shortliffe and Buchanan methodology [10] to create an evolution that includes fuzzy sets and membership functions that are contextualized for each spectral type. The applied inference method is Max-product, which combines the influence of all the active rules and produces a smooth, continuous output. In our approach, the credibility factor of each rule has also been considered as another truth value. The defuzzification of the data into a crisp output was accomplished by the fuzzy-centroid method [11]. With this mixed strategy, we achieved a remarkable adaptation to human reasoning, able to successfully handle the imprecision and uncertainty implicit in the manual classification process. In addition, we obtained the spectral classification of stars with a probability value that indicates the grade of confidence. Our final system is able to classify stars with a success rate very similar to the agreement percentage between experts in the field (approximately 80%).

This part of the spectral classifier was developed in OPS/R2 [8] and integrated with the analyzer by means of dynamic link libraries (DLL).

An additional research topic consisted in improving the implemented system by applying the results of the best neural models, and will be described in the next sections. The weights of the output layer units were analyzed so as to determine, for each spectral type, which input parameters have more influence on the output. The normalized values of the higher weights were included in the expert system in the shape of credibility factors of the rules that correspond to the most influential parameters for each spectral type. This modification of the reasoning rules (using the weights values of the trained neural networks) resulted in a slightly significant improvement of the performance of the original expert systems (around 2%).

4.2 Artificial Neural Networks

The neural networks of this approach are based on both supervised and nonsupervised learning models [12]. In particular, Backpropagation, Kohonen and Radial Basis Functions (RBF) networks were implemented.

We have tested three backpropagation learning algorithms (standard, momentum and quick) for the spectral types, spectral subtypes and luminosity classes.

We have also tested RBF networks; networks based on Radial Basis Functions (RBF) combine non-supervised learning for hidden units and supervised learning in the output layer. The hidden neurons apply a radial function (generally Gaussian) to the distance that separates the input vector and the weight vector that each one stores, called centroid.

Finally, we have also implemented Kohonen networks. The Self-Organizing Map (SOM) algorithm of Kohonen is based on non-supervised learning. SOMs are a unique class of neural networks, since they construct topology-preserving mappings of the training data where the location of a unit carries semantic information [13].

The training, validation and testing patterns that are presented to the neural networks were obtained automatically by adding the necessary functions to the spectral analyzer developed in the expert systems approach. Once the input values are obtained by the spectral analyzer, they must be normalized and presented to the neural networks. Our study standardizes the inputs of the network by means of a contextualised and specific sigmoidal function for each parameter. This function normalizes the input parameters in the [0, 1] interval and centers and scales the distribution function of each parameter properly. The different topologies that were implemented for the three learning algorithms are shown in Table 3.

The backpropagation topology that has resulted in a better performance corresponds to a network trained with 25 spectral parameters as input layer and three hidden layers of 10, 5 and 3 units. The best results for Kohonen networks were achieved by maps of 12x12 units. As for the RBF networks, the best topology corresponds to a network trained with 25 spectral parameters as input layer and 8 neurons in the hidden layer.

4.3 Statistical Clustering Techniques

In order to refine the classifications made by artificial neural networks and expert systems, we have implemented statistical clustering techniques and applied them to the problem of spectral classification. In particular we have implemented the K-means, Max-Min and Isodata non-hierarchical clustering methods [14].

This approach uses the spectral parameters, obtained through the morphological analysis algorithms, as well as the full spectra. In addition, two different versions of each algorithm with 6 and 12 initial clusters were implemented.

Although the implemented clustering methods have achieved remarkable success rates in stellar spectra classification, this technique was mainly applied to analyze the sensibility of the spectral parameters that were used to classify the stellar spectra.

Network	Input Patterns	Hidden Layer
BP Type	Spectral parameters	10
BP Type	Spectral parameters	5x5
BP Type	Spectral parameters	10x10
BP Type	Spectral parameters	10x5x3*
BP Type	659 flux values	100x50x10x3
BP Luminosity	Spectral parameters	10x10
BP Luminosity	659 flux values	100x50x10x3
RBF Type	Spectral parameters	16
RBF Type	Spectral parameters	8*
RBF Type	Spectral parameters	4
RBF Type	659 flux values	124
RBF Luminosity	Spectral parameters	8
RBF Luminosity	659 flux values	124
Kohonen Type	Spectral parameters	2x2
Kohonen Type	Spectral parameters	12x12*
Kohonen Type	Spectral parameters	24x24
Kohonen Luminosity	Spectral parameters	2x2

 Table 1. Topologies tested for Backpropagation (BP), Kohonen and RBF networks (* shows best networks).

5 Results

This section makes the final comparison between the three applied global approaches: expert systems, clustering techniques and artificial neural networks. We selected the neural models of each type with the best performance and classified, by means of clustering algorithms and expert systems, the 100 spectra that were used to test these networks. Figure 1 contrasts the behaviour of the automatic techniques and that of two human experts who collaborated on this project.

The Backpropagation and RBF networks, as well as K-means and Isodata algorithms, obtained a high success rate of approximately 95%. The Kohonen model obtained a low success rate in all its implementations, which could be due to the size of the training set: this network type must cluster the data and therefore needs a training set that is large enough to extract similarities and group the data.

Although the final results for the proposed classification methods seem to be similar, an exhaustive study has revealed some interesting peculiarities; for example, we have observed that each technique reached its worst results for the B and M spectral types, i.e. the hottest and coolest stars respectively, and indeed, most of the grouping algorithms include these spectra in the same cluster. This fact led us to review the spectral parameters that were being used to design the models: we discovered that B stars usually present great emission lines in zones where a molecular band is expected, which means that the automatic techniques are unable to differentiate between them. Our hybrid approach tries to solve these problems by making a previous global classification of the star and then selecting the best method to classify the spectra.



Fig. 1. Final performance for 100 testing spectra

This final strategy consists of choosing, among all the described techniques, those methods that present the best performance for each classification level. The final system is mainly based on an expert system that determines the global type of each star and that, according to the type, sends the spectra to different neural networks or clustering algorithms in order to obtain their spectral type as well as their luminosity level. The expert system classification is also used, as an additional information, for those cases in which the other methods are unable to discriminate. The final implemented system allows the users to select the spectra, visualize them, perform different analyses and classify as many spectra as they want in a fast, comfortable and simple way, which is the global objective of this computational approach.

6 Conclusions

This paper has proposed a hybrid and cooperative approach to the problem of MK classification of stars. Our contribution is based on the development of an unattended system that morphologically analyzes and automatically classifies the optical spectra of stars.

We described several artificial intelligence models and analyzed their performance and results to discover the best approach to the classification of each type of spectrum. In our research, we combined signal processing techniques, expert systems, artificial neural networks and clustering algorithms.

The best techniques reached a success rate of approximately 95% for a sample of 100 testing spectra, which, compared to manual classifications, corresponds to a performance increase of approximately 10% (since the experts reached an agreement percentage of approximately 87% of the spectra).

By using the additional classification information provided by the clustering techniques, we have opened a new research line for the refinement of automatic classifications, especially for spectral types B and M; the implemented clustering techniques allow us to perform a sensibility analysis of the spectral parameters used to classify stellar spectra in the neural networks and expert systems approach.

Finally, all the artificial intelligence techniques were integrated into a hybrid system that has resulted in a versatile and flexible automatic method for the classification of stellar spectra. In this way, the proposed system can achieve a better adaptation to the classification problem, since each spectrum is processed with the most appropriate technique according to its specific features.

For the evaluation period of the proposed models, we could count on the essential collaboration of experts from the area of Astronomy and Astrophysics of the University of A Coruña.

At present, we are working on our stellar database and we are developing a web site to make the automatic classification system available through the Internet so as to allow world-wide users to analyze and classify stellar spectra online in a fast, efficient and comfortable way.

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